

LISA Astrophysics Working Group Meeting, MPA, Nov 2024

Identifying eccentric black hole mergers in dynamical formation environments

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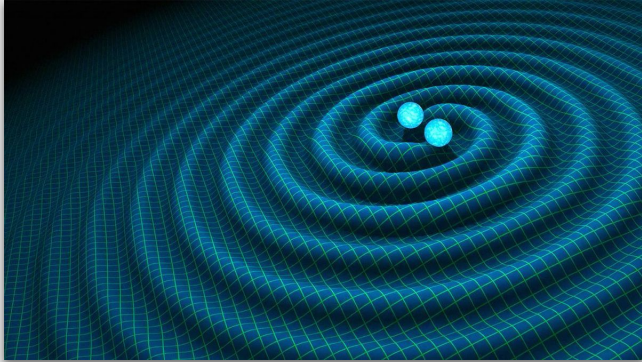


VILLUM FONDEN



Motivation: different formation channels

Isolated formation



Dynamical formation

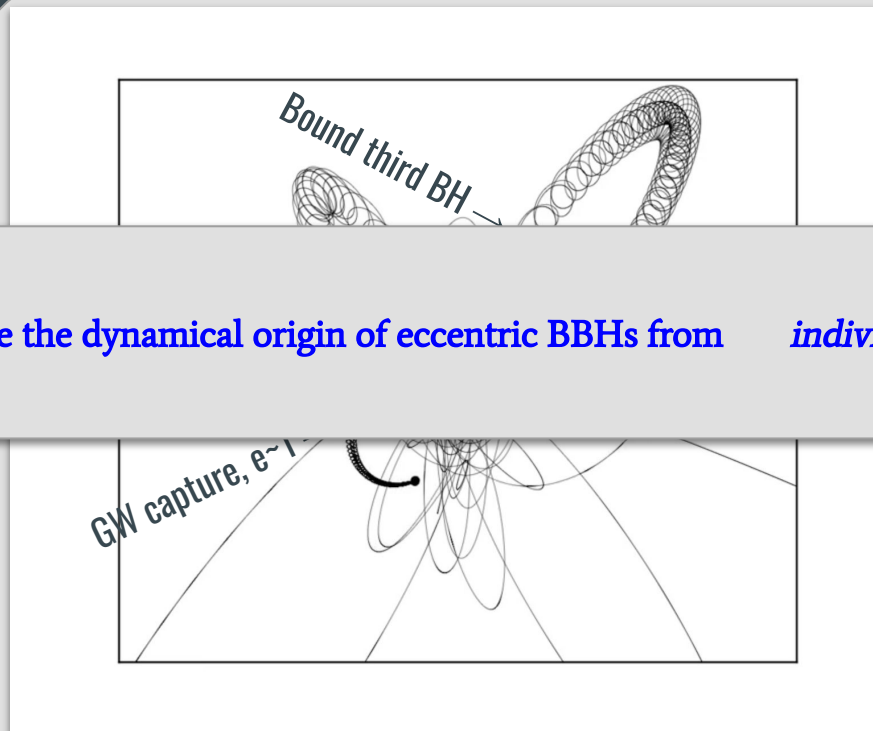
Globular clusters



Active galactic nuclei



Motivation: the dynamical channel



How can we probe the dynamical origin of eccentric BBHs from *individual* GW events?

Fig. 1: example of a 3-body scattering.

Phase shift

$$\Delta\phi(e) \approx \frac{288\sqrt{2}}{85^2 g(1)^{13/2}} \frac{c^9}{G^{9/2}} \times \frac{m_3}{R^2} \frac{r_0^{13/2}}{m_1^2 m_2^2 m_{12}^{3/2}} \\ \times e^{78/19} (1 - e^2)^{1/2} g(e)^{13/2}$$

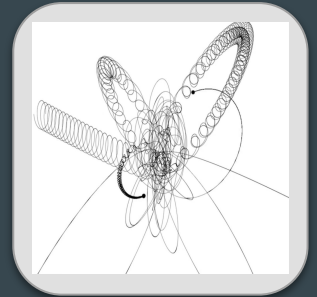
Phase shift peaks when $e \sim 0.95!$

How high can the phase shift get?

Take your favourite few-body simulation code

Simulate many binary-single interactions typical for clusters

Calculate the phase shift for those in triple configuration



How high can the phase shift get?

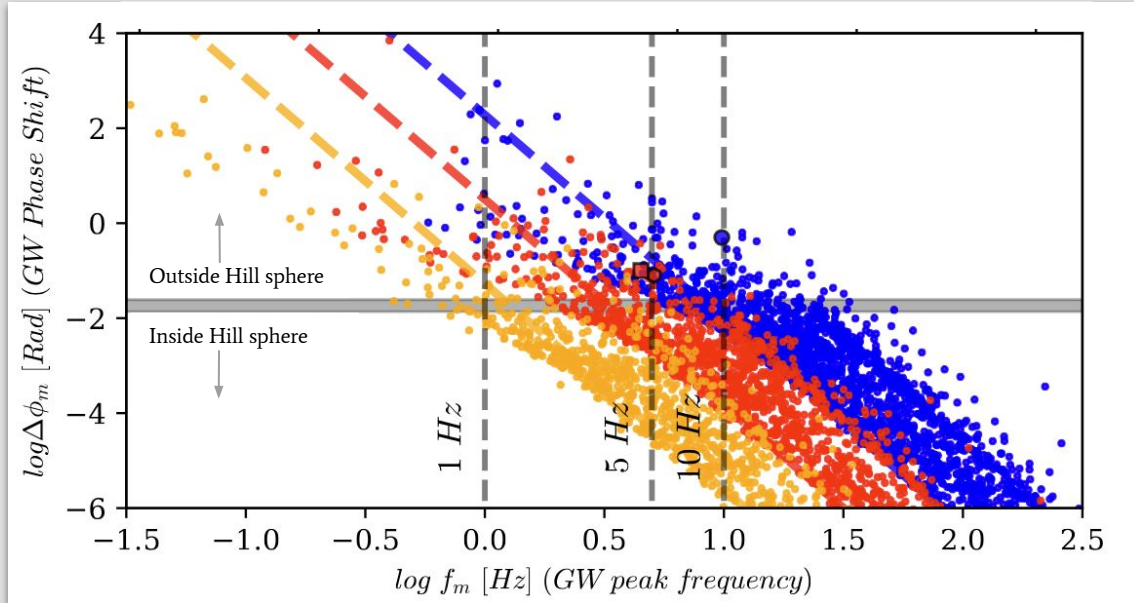


Fig. 4: maximum phase shift as a function of the peak GW frequency at formation of the binary. We use an equal mass triple of 20 solar masses. The different colours represent different initial semi-major axes: from 0.01 AU (blue) to 0.1 AU (red) and 1 AU (orange). The horizontal lines are the astrophysically expected upper limits.

Summary

How can we probe the dynamical origin of eccentric BBHs from *individual* GW events?

GW phase shift!



Can map the environment in which the binary formed

3G detectors such as LISA/ET/CE may be able to detect this environmental effect

Questions?



Contact me at [kai.hendriks@nbi.ku.dk!](mailto:kai.hendriks@nbi.ku.dk)

Astrophysical scenarios: 3-body scatterings

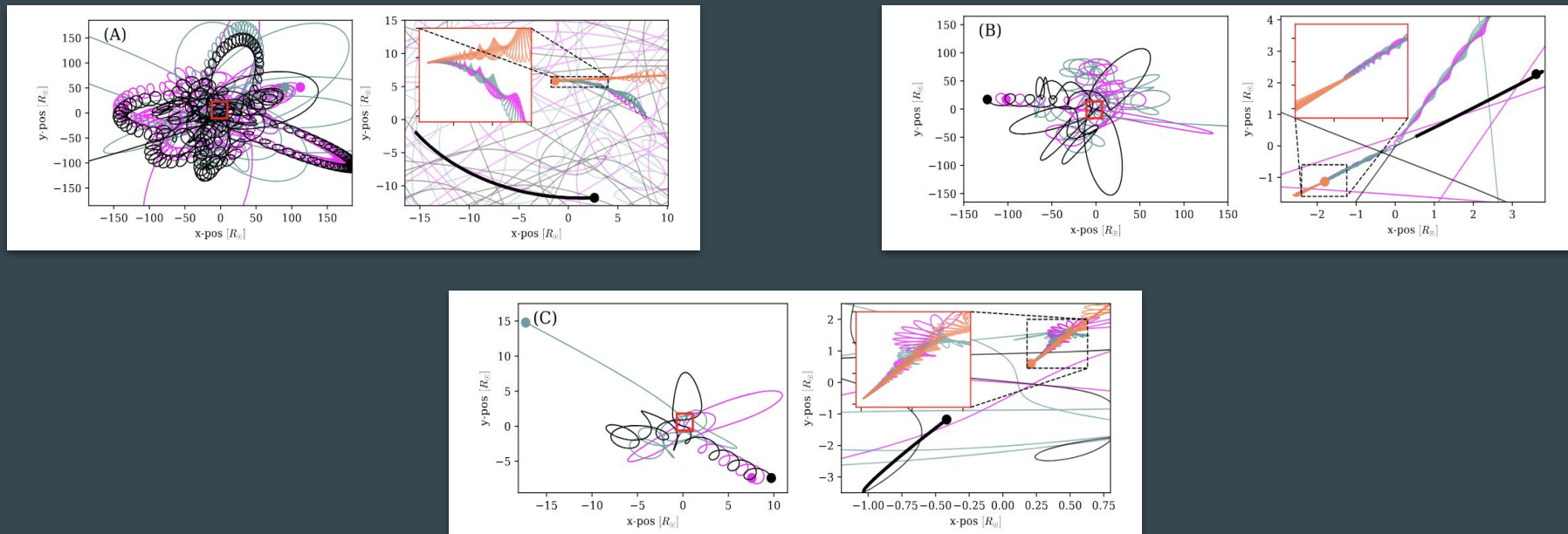


Fig. 13: examples of 3-body scatterings that lead to phase shifts higher than the theoretical maximum.

Astrophysical scenario: 3-body scatterings

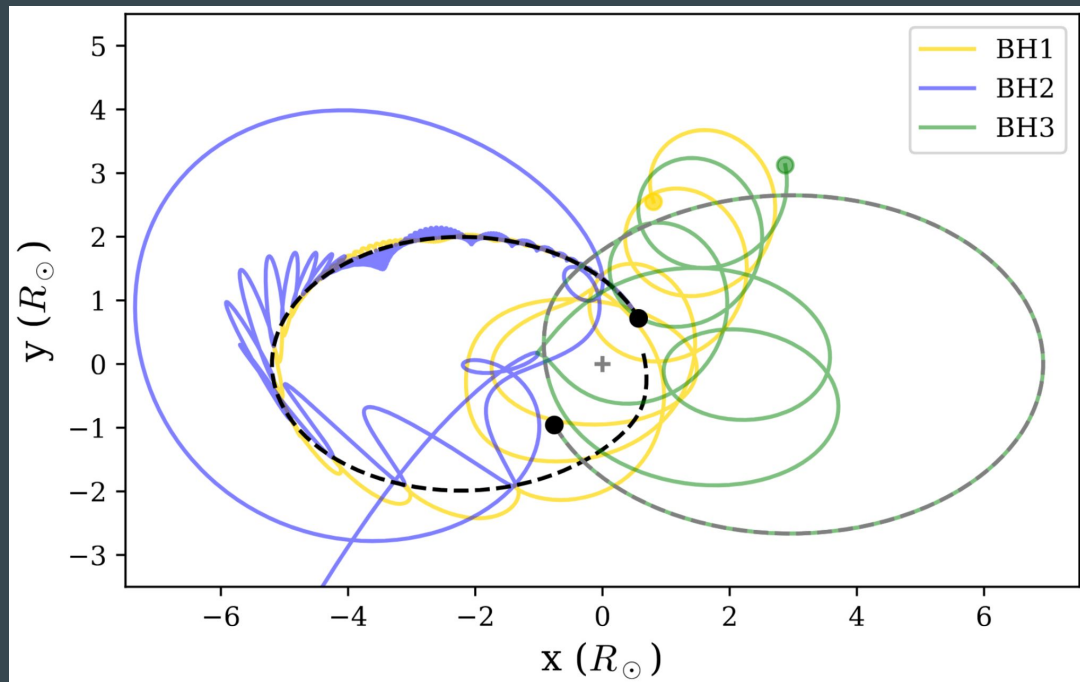


Fig. 8: 3-body scattering (5, 15 and 15 M_{sun}) resulting in an inspiralling and merging binary on a bound orbit around a third object.

Astrophysical scenario: 3-body scatterings

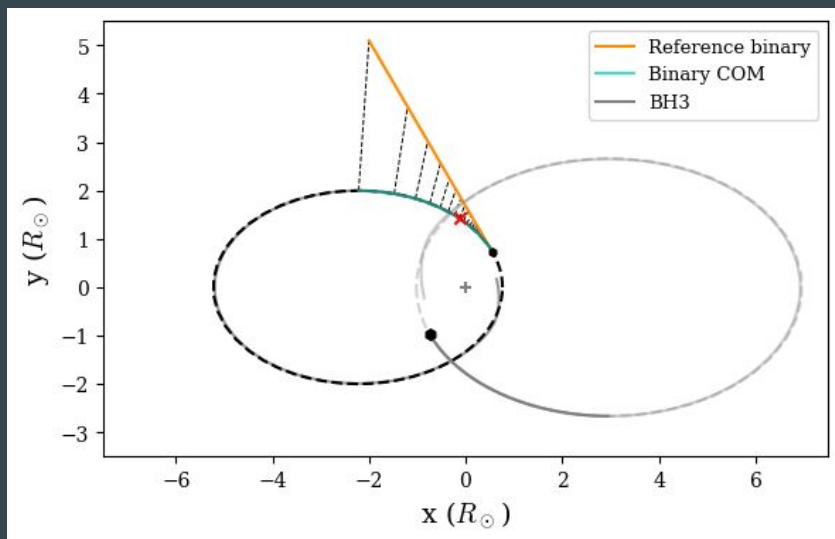


Fig. 9: binary COM, reference trajectory and perturber trajectory of the scattering in question. We can extract the Rømer delay and phase shift from this.

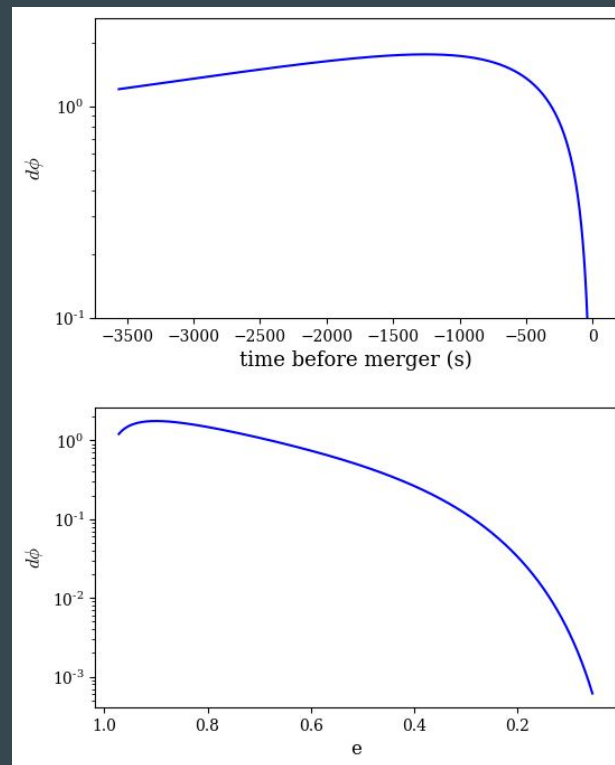


Fig. 10: phase shift of this scattering, as a function of time (top) and binary eccentricity (bottom).

Phase shift: eccentric outer orbit

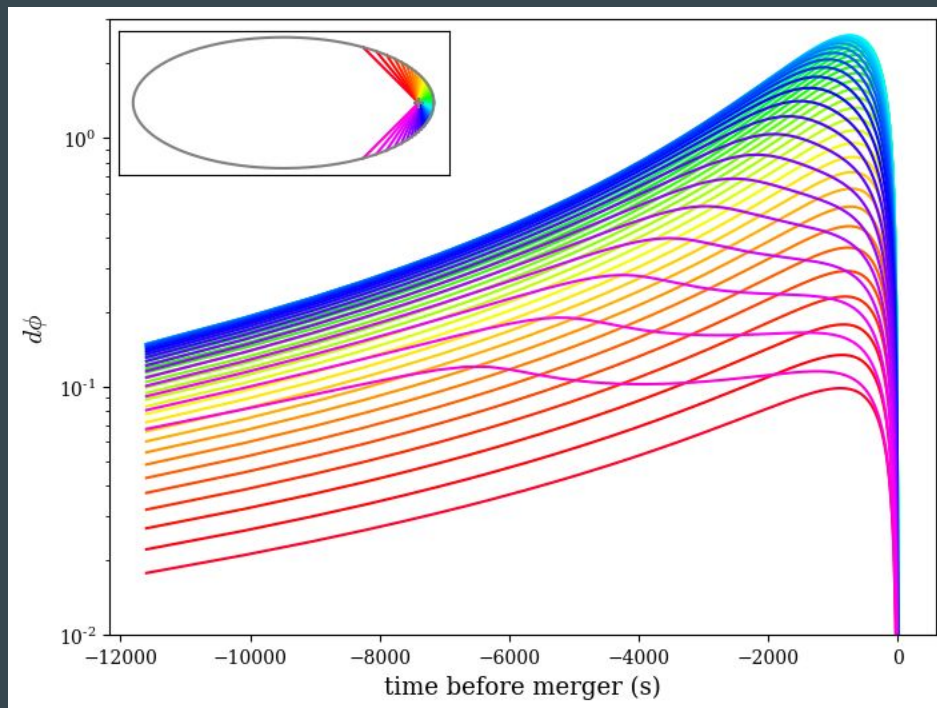
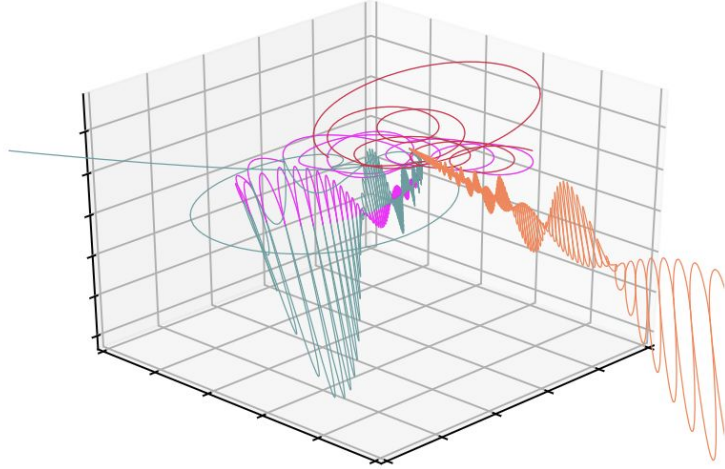


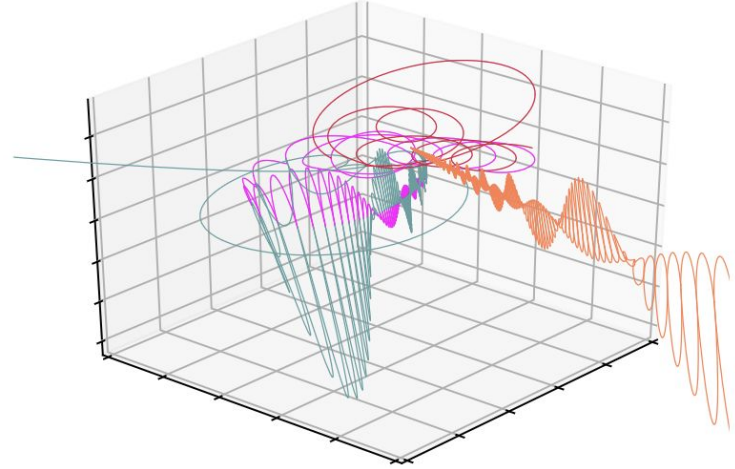
Fig. 7: phase shift as a function of time, for different realisations of f_m , ranging from $-\frac{3}{4}\pi$ to $\frac{3}{4}\pi$. We still use an eccentric $5 M_\odot$ equal-mass binary, inspiralling on an eccentric orbit ($e=0.9$, $a=30 R_\odot$) around a $100 M_\odot$ perturber. The binary assembles at a semi-major axis $a_0=1.3 R_\odot$ and $e_0 = 0.9999$.

Stereoscopic images

STEREOSCOPIC IMAGE A



STEREOSCOPIC IMAGE B



Phase shift: analytical approximation

- Problem: no analytical description when outer orbit is eccentric

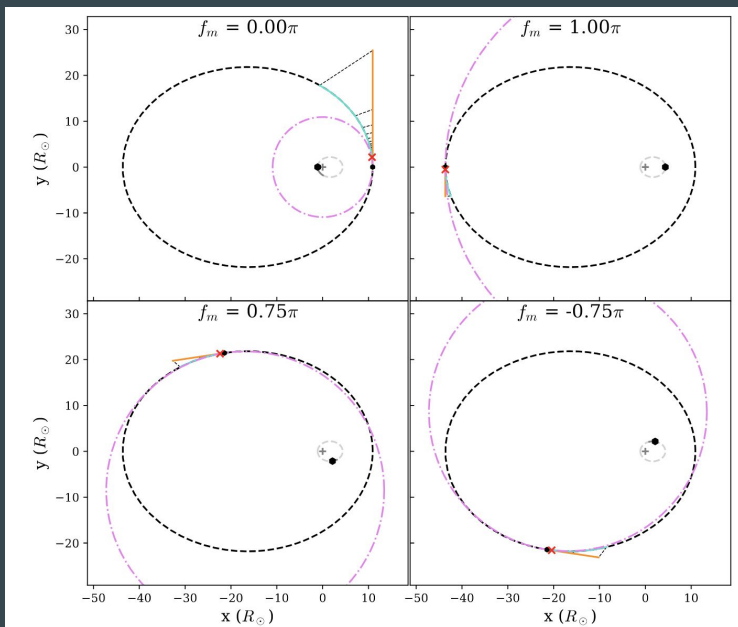


Fig. 9: trajectories and phase shift of an eccentric $5 M_{\odot}$ equal-mass binary, inspiralling on an eccentric orbit ($e=0.9$, $a=30 R_{\odot}$) around a $100 M_{\odot}$ perturber. The binaries assemble at a semi-major axis $a_0=1.3 R_{\odot}$ and $e_0 = 0.9999$, for 4 different outer phases at merger.

$$\Delta\phi(e) \approx \frac{288\sqrt{2}}{85^2 g(1)^{13/2}} \frac{c^9}{G^{9/2}} \times \frac{m_3}{R^2} \frac{r_0^{13/2}}{m_1^2 m_2^2 m_{12}^{3/2}} \times e^{78/19} (1-e^2)^{1/2} g(e)^{13/2}$$

Phase shift: circular outer orbit

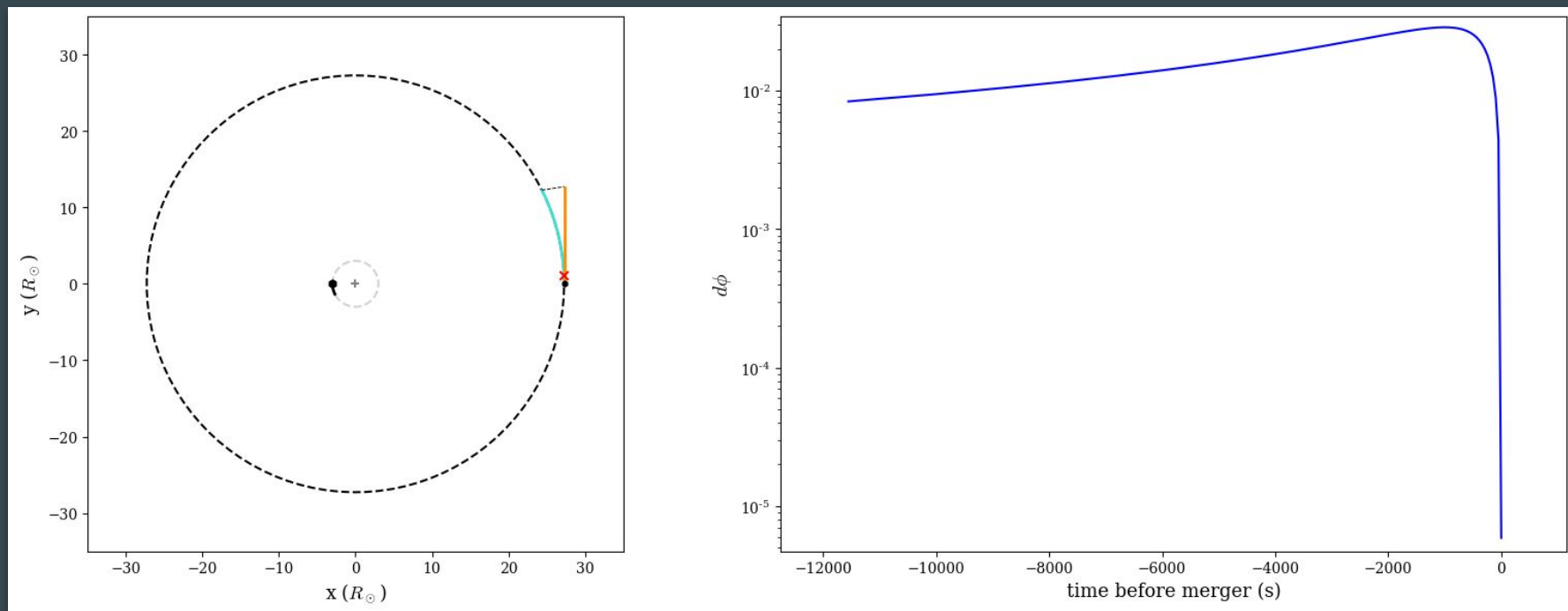


Fig. 6: trajectory and phase shift of an eccentric $5 M_\odot$ equal-mass binary, inspiralling on a circular orbit ($30 R_\odot$) around a $100 M_\odot$ perturber. The binary assembles at a semi-major axis $a_0 = 1.3 R_\odot$ and $e_0 = 0.9999$.

Phase shift: effect of outer eccentricity

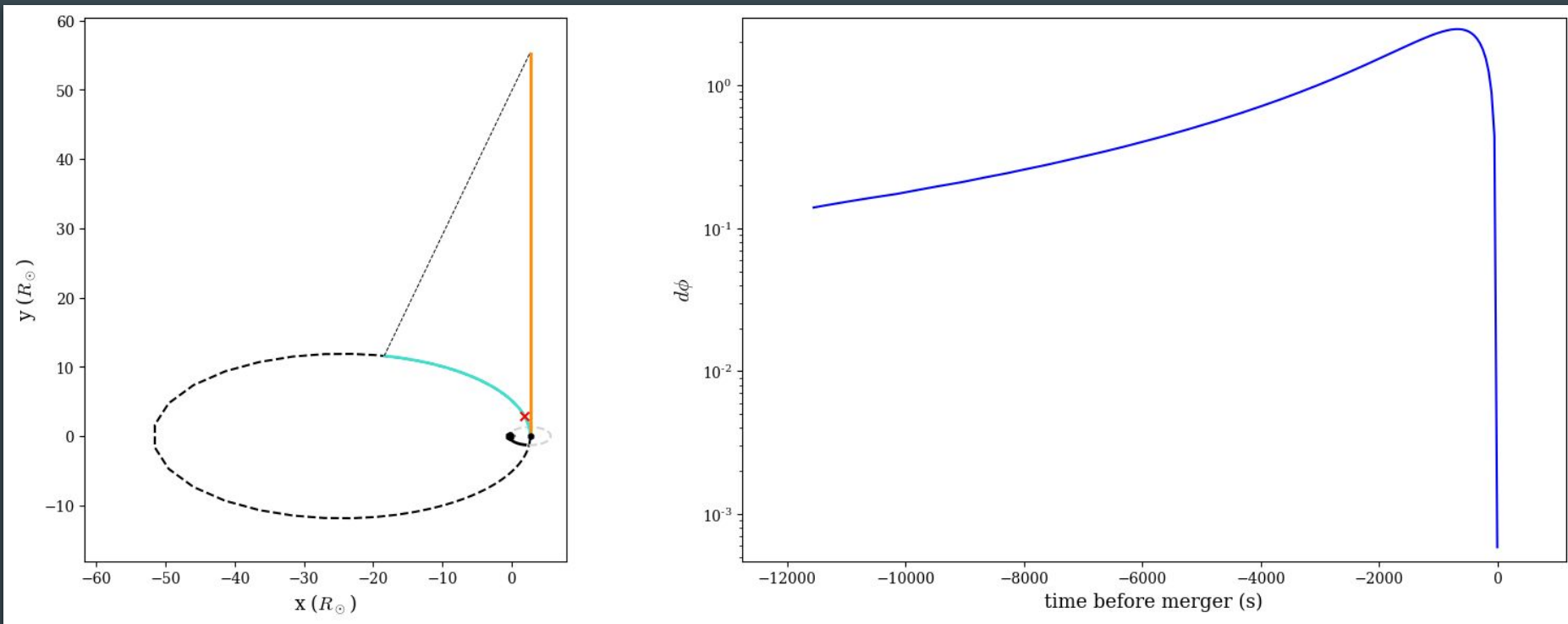


Fig. 8: trajectory and phase shift of an eccentric $5 M_\odot$ equal-mass binary, inspiralling on an eccentric orbit ($e=0.9$, $a=30 R_\odot$) around a $100 M_\odot$ perturber. The binary assembles at a semi-major axis $a_0=1.3 R_\odot$ and $e_0 = 0.9999$, and merges at pericentre ($f_m=0$).

Phase shift: eccentric outer orbit

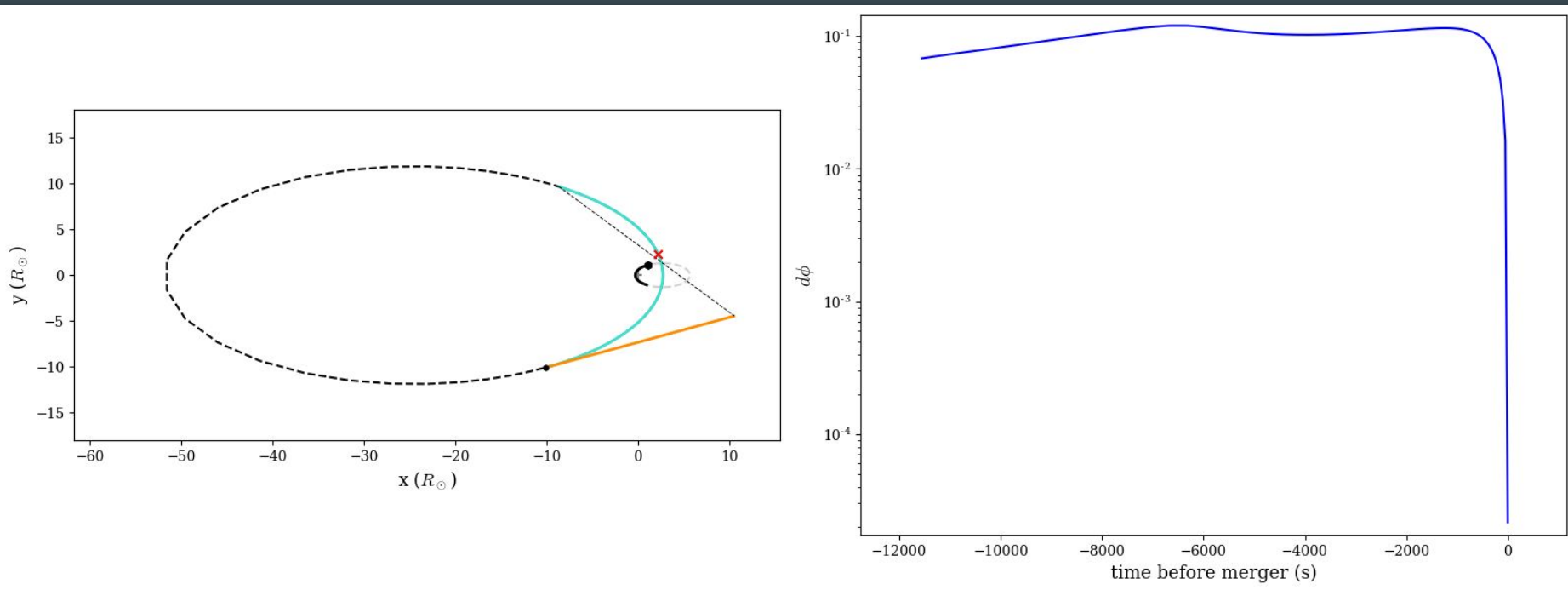


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Phase shift: effect of the outer eccentricity

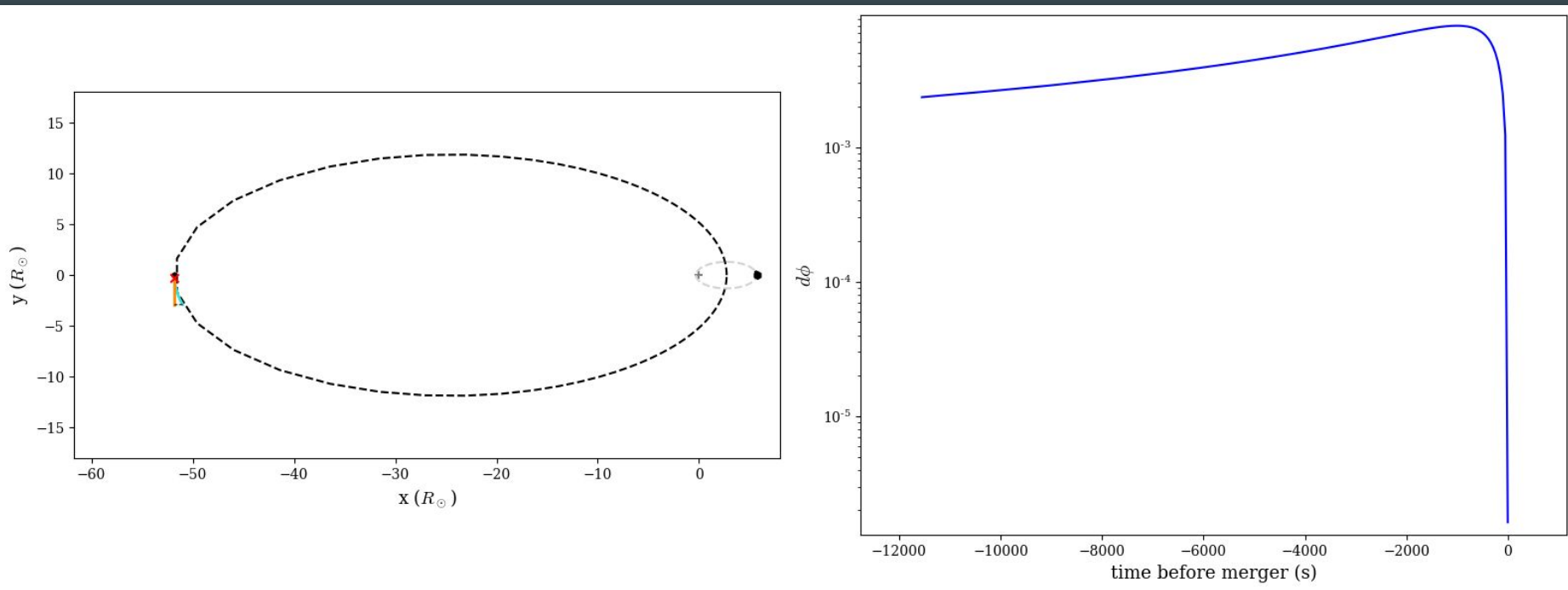


Fig. 9: trajectory and phase shift of an eccentric $5 M_\odot$ equal-mass binary, inspiralling on an eccentric orbit ($e=0.9$, $a=30 R_\odot$) around a $100 M_\odot$ perturber. The binary assembles at a semi-major axis $a_0=1.3 R_\odot$ and $e_0 = 0.9999$, and merges at apocentre ($f_m = \pi$).

Astrophysical scenario: 3-body scatterings

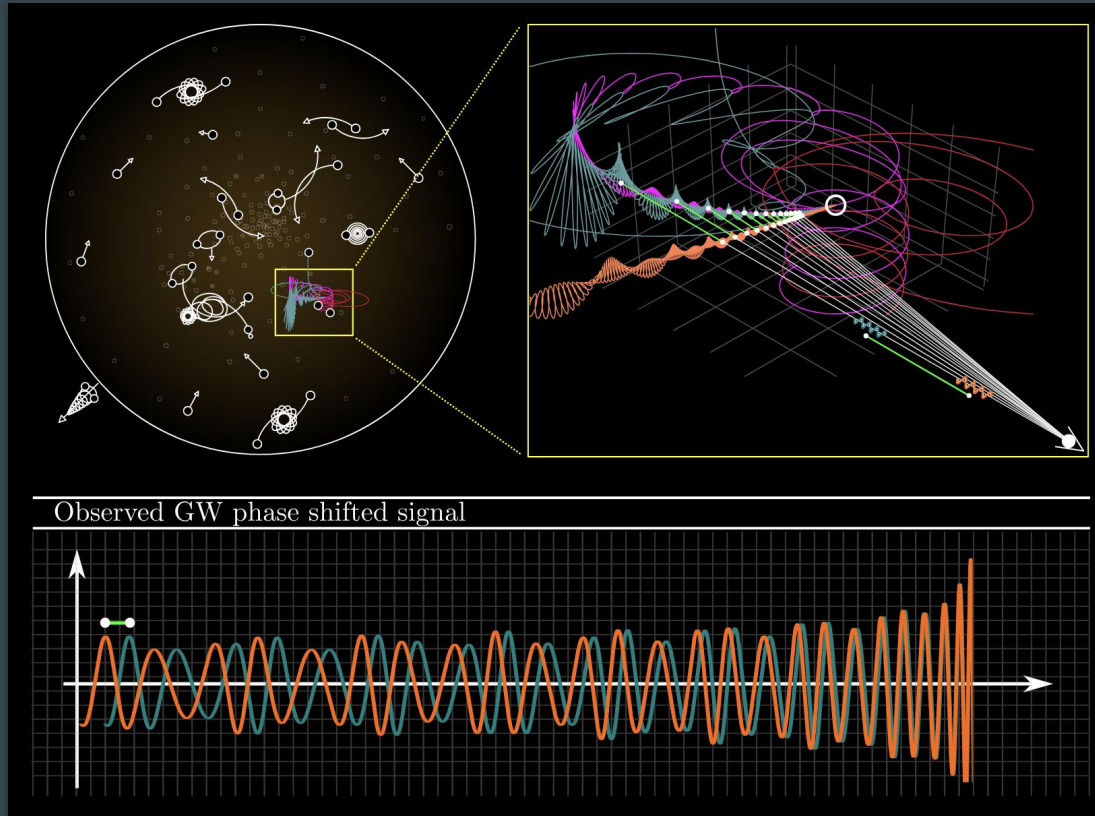


Fig. 11: 3-body scatterings with GW mergers in a stellar cluster..