

# Full and repeated TDEs

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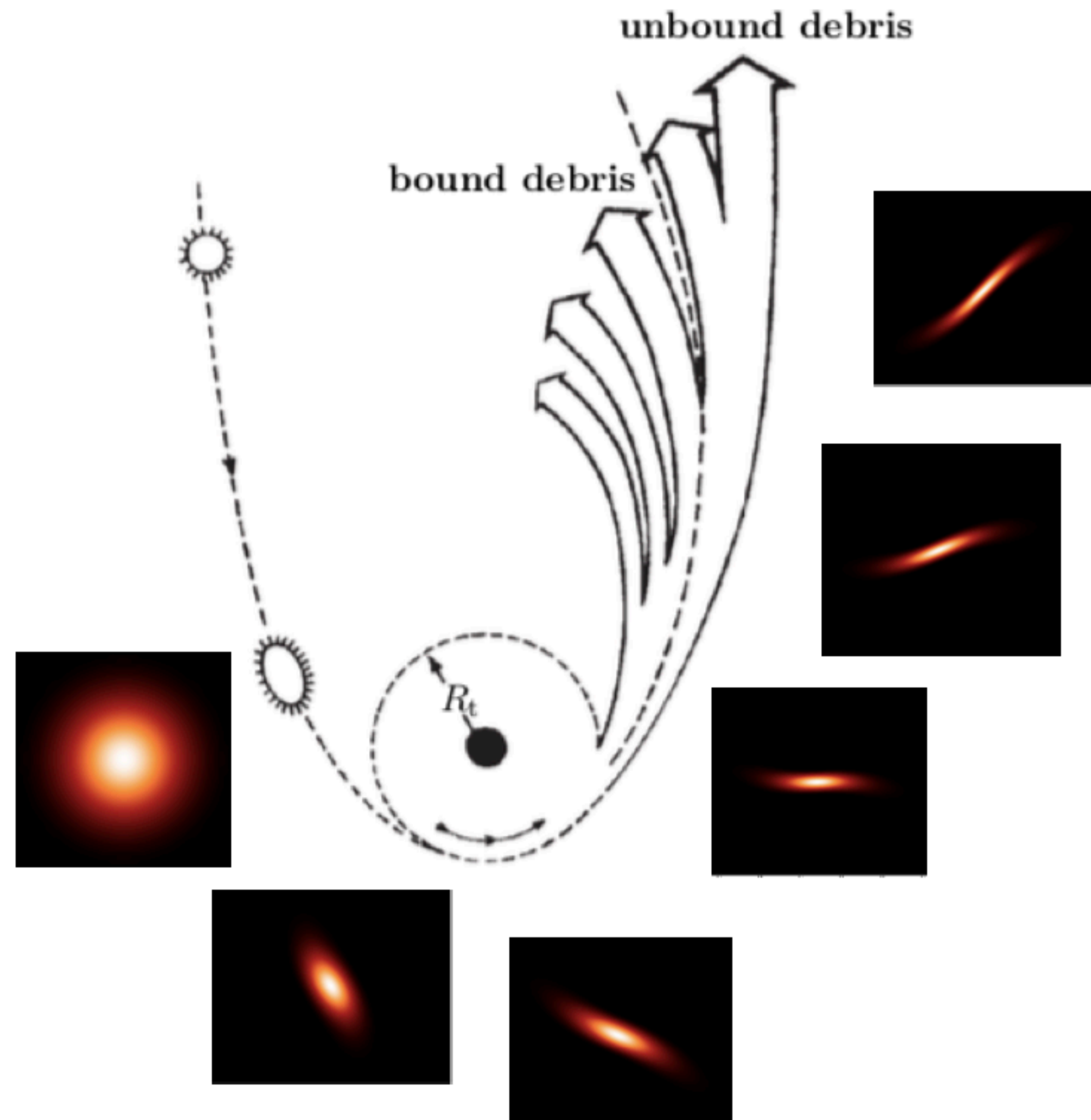
LISA AstroWG meeting, MPA

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In collaboration with: Dr. Luca Broggi, Prof. Sesana and Prof. Rossi



# TDEs



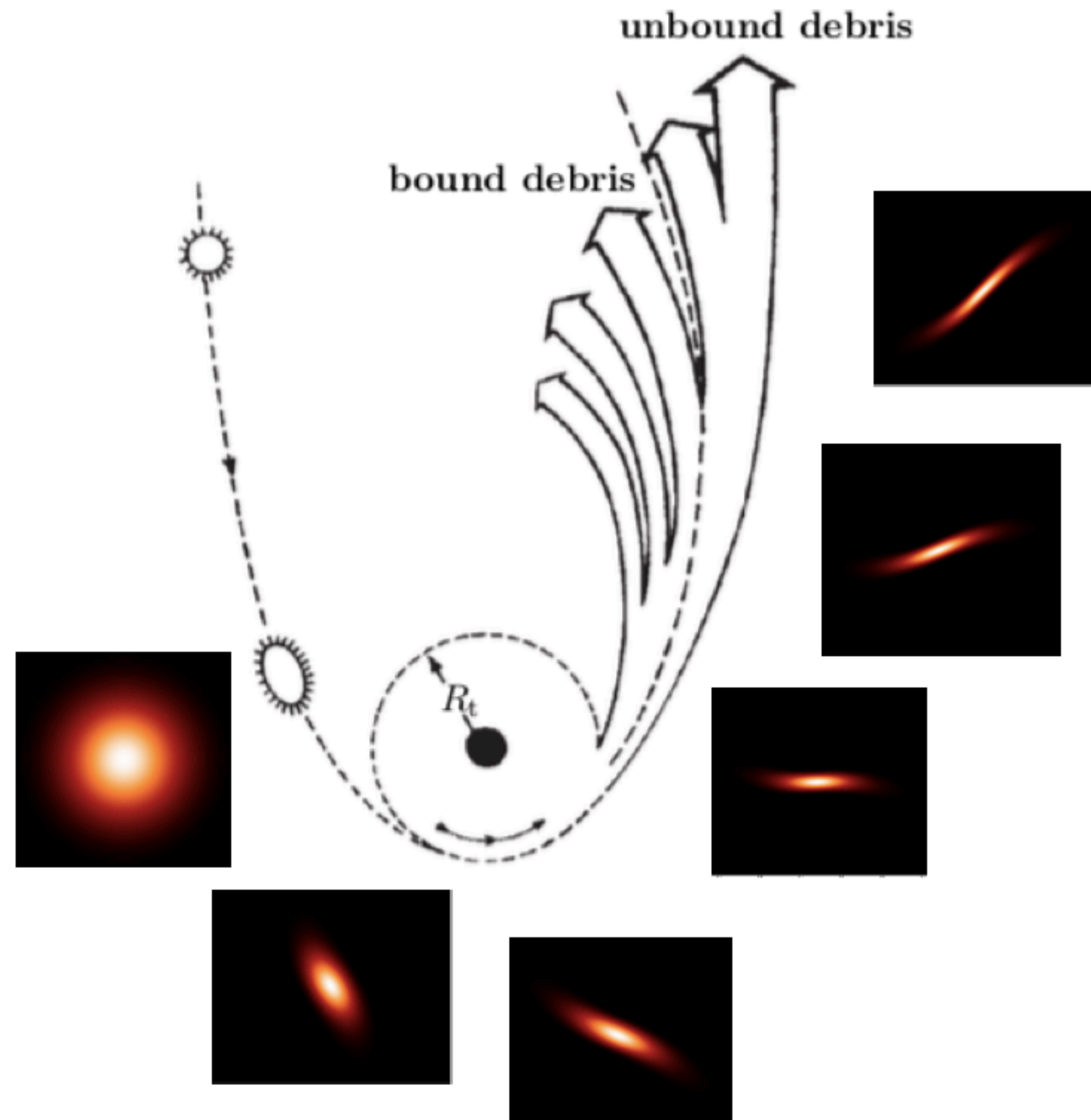
Stars tidally disrupted by BH tides (Rees88, Phinney89. Recent:: Ryu+20, Rossi+21, Bonnerot & Stone 21)

Multimessenger emitters

- Luminous electromagnetic flares (reviews: Saxton+20, vanVelzen+20, Alexander+20)
- High energy neutrinos (Hayasaki21, Stein22, Reusch+22,)
- GWs (Kobayashi+04, **Toscani**+19,20,22,23, Pfister, **Toscani**+22)

(Original image from Rees88. Snapshots produced by Toscani using PHANTOM (Price+18))

# TDEs



- Refine estimates of Pfister, Toscani+22 and Toscani+20 considering all the harmonics of the signal (formalism by Berry&Gair10)
- Distinction between full TDEs and repeated partial TDEs

(Original image from Rees88. Snapshots produced by Toscani using PHANTOM (Price+18))

fTDEs: main sequence stars

$$\frac{d^4 \dot{N}_{\text{det}}^{\text{fTDEs}}}{dz dM_{\bullet} dM_* dR_p} \approx \frac{d^2 \Gamma(M_{\bullet})}{dM_* dR_p} \times \Phi(M_{\bullet}, z) \times \frac{4\pi\chi^2(z)}{H(z)} \times \Theta(z, M_{\bullet}, M_*, R_p)$$

fTDEs: main sequence stars

$$\frac{d^4 \dot{N}_{\text{det}}^{\text{fTDEs}}}{dz dM_{\bullet} dM_* dR_p} \approx \frac{d^2 \Gamma(M_{\bullet})}{dM_* dR_p} \times \Phi(M_{\bullet}, z) \times \frac{4\pi\chi^2(z)}{H(z)} \times \Theta(z, M_{\bullet}, M_*, R_p)$$

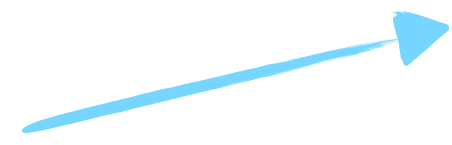
Massive BH mass function  
(Davidzon et al. 2017, Reines & Volonteri)

Comoving volume  
(Hogg 1999)

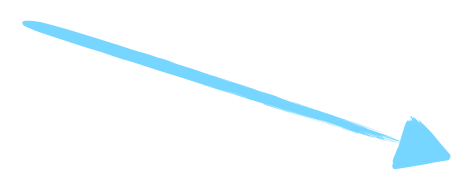
fTDEs: main sequence stars

$$\frac{d^4 \dot{N}_{\text{det}}^{\text{fTDEs}}}{dz dM_{\bullet} dM_* dR_p} \approx \frac{d^2 \Gamma(M_{\bullet})}{dM_* dR_p} \times \Phi(M_{\bullet}, z) \times \frac{4\pi\chi^2(z)}{H(z)} \times \Theta(z, M_{\bullet}, M_*, R_p)$$

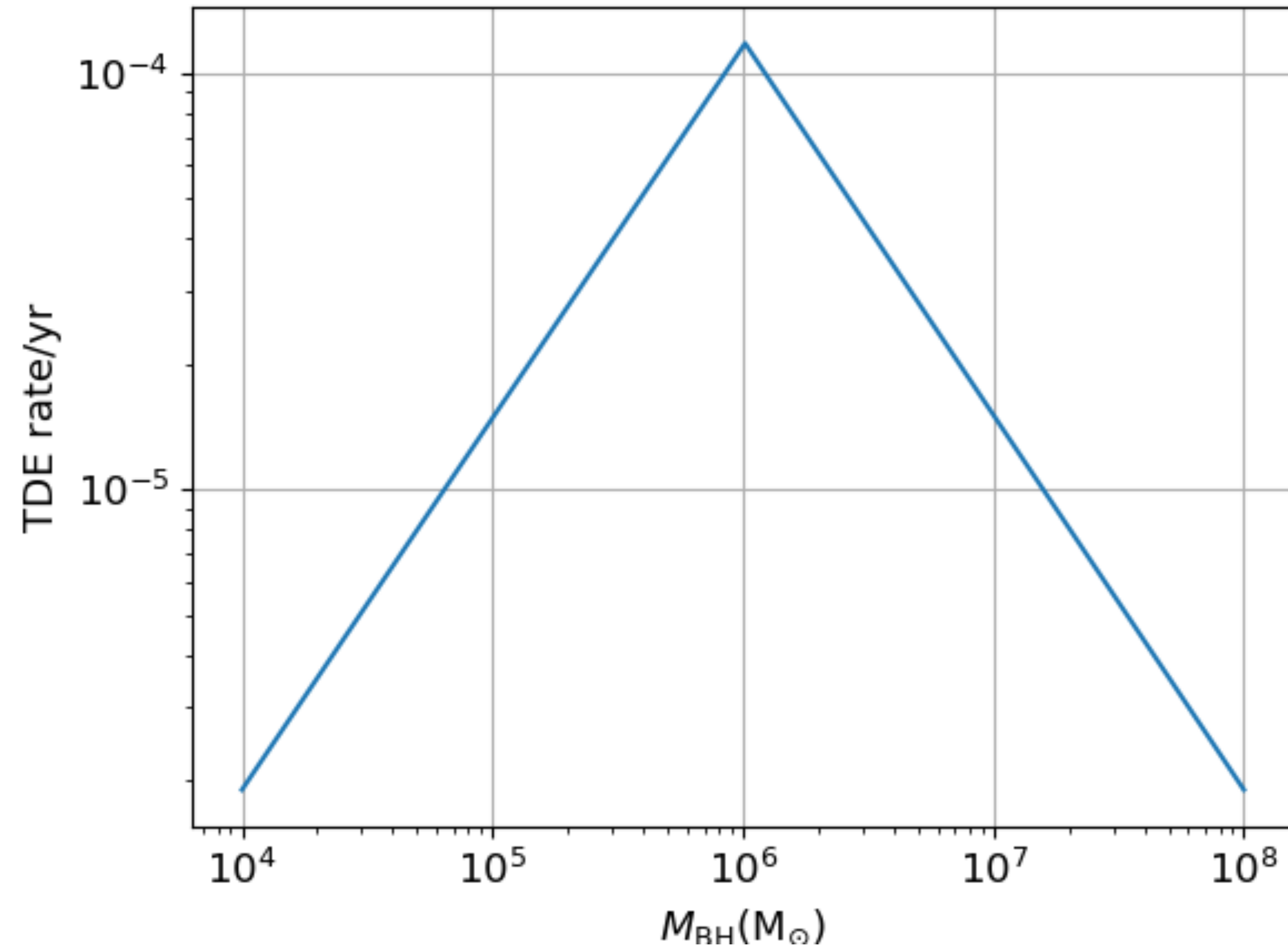
$$\frac{d^2 \Gamma(M_{\bullet})}{dM_* dR_p}$$



Chang et al. 2024



Broggi et al. 2024



fTDEs: main sequence stars

$$\frac{d^4 \dot{N}_{\text{det}}^{\text{fTDEs}}}{dz dM_{\bullet} dM_* dR_p} \approx \frac{d^2 \Gamma(M_{\bullet})}{dM_* dR_p} \times \Phi(M_{\bullet}, z) \times \frac{4\pi\chi^2(z)}{H(z)} \times \Theta(z, M_{\bullet}, M_*, R_p)$$

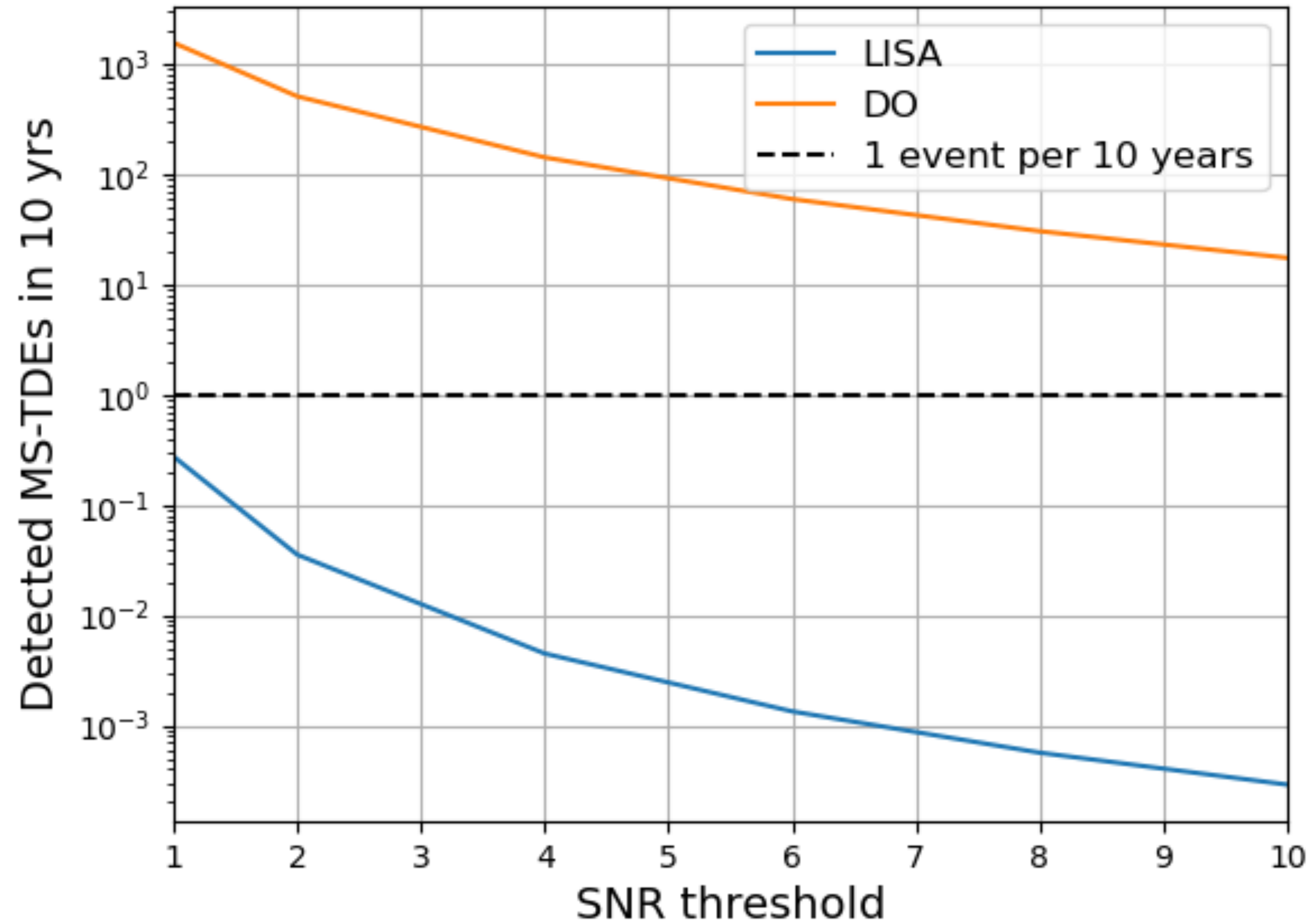
$$\Theta(z, M_{\bullet}, M_*, R_p) \longrightarrow \text{SNR}^2 = 4 \int_0^{\infty} df \frac{\tilde{h}(f)^2}{S_{n_n}(f)}$$

Harmonics

Instrument

## fTDEs: main sequence stars

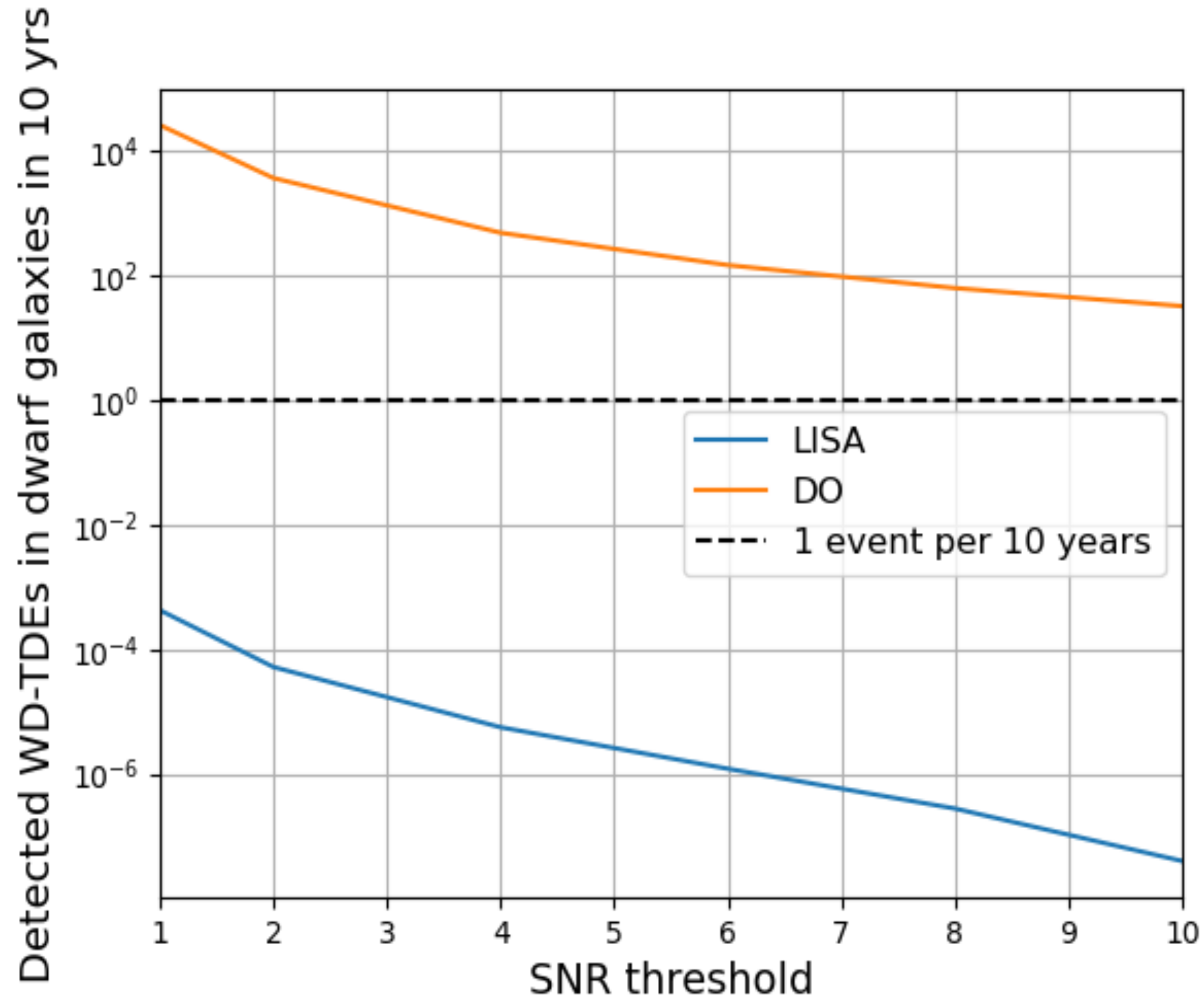
$$0.1M_{\odot} \leq M_* \leq 10M_{\odot}, 10^4M_{\odot} \leq M_{\bullet} \leq 10^7M_{\odot}, 10^{-4} \leq z \leq 3$$



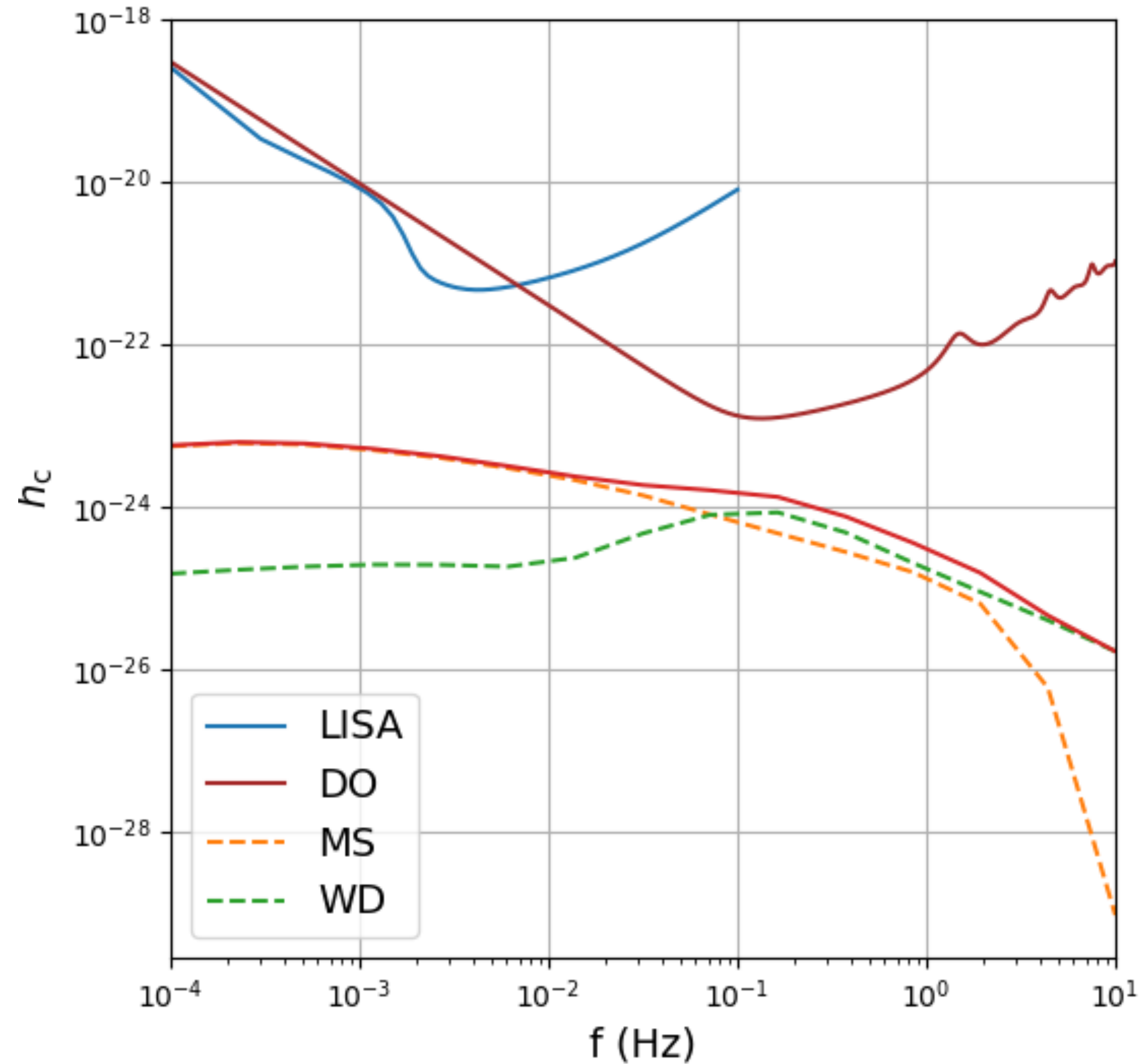


# fTDEs: white dwarfs

$$M_* = 0.5M_\odot, 10^3 \leq M_\bullet \leq 10^5 M_\odot, 10^{-4} \leq z \leq 3$$



# GW background from fTDEs



$$h_{c,\text{pop}}^2 = \frac{G}{c^3 \pi^2} \times \frac{1}{f} \times \int_0^\infty dz \frac{d\dot{N}^{\text{tde}}}{dz} \times \frac{1}{\chi^2(z)} \frac{1}{1+z} \left( \frac{dE}{df} \right)$$

## rpTDEs: background

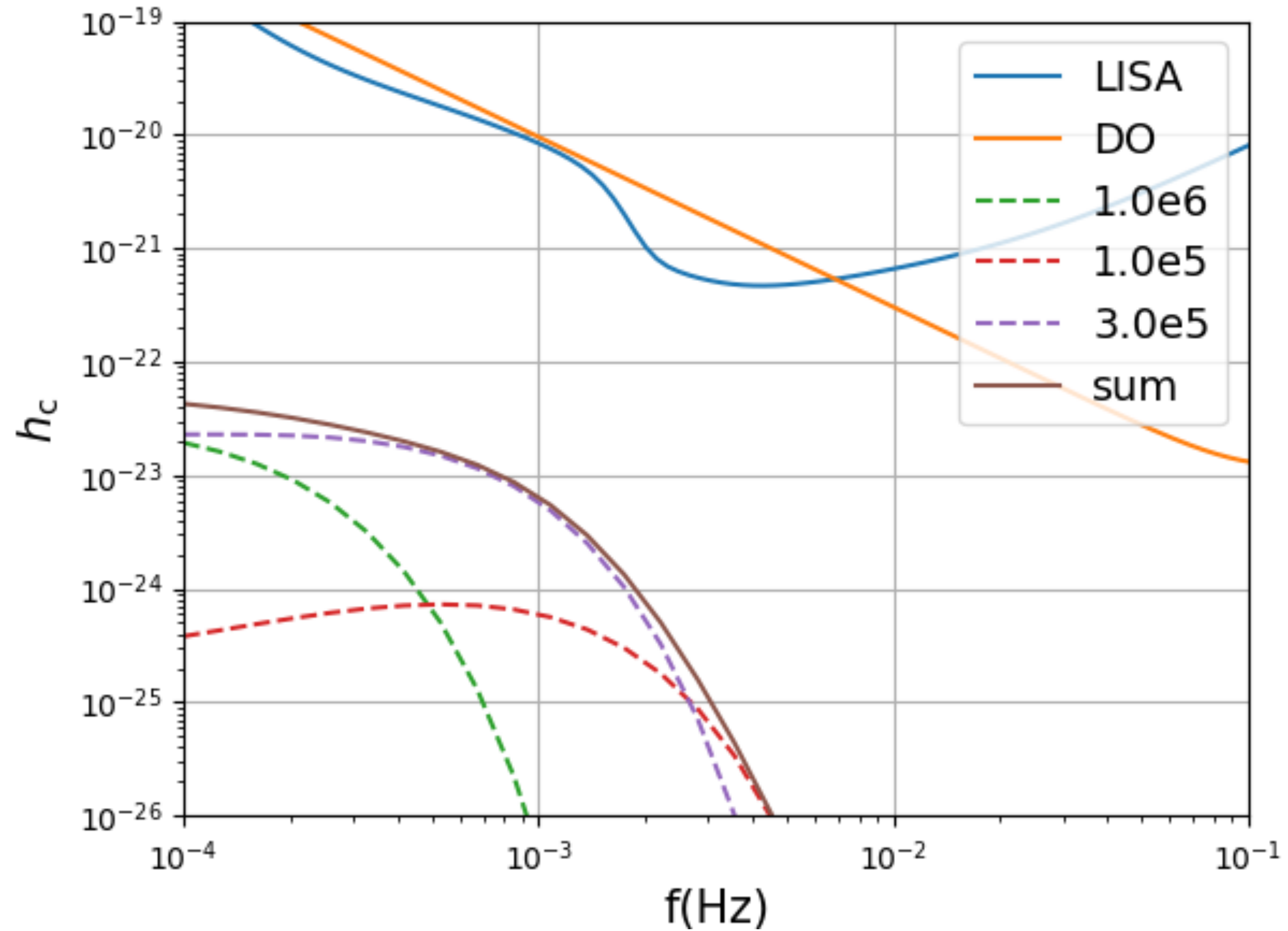
$$h_{c,\text{pop}}^2 = \frac{G}{c^3 \pi^2} \times \frac{1}{f} \times \int_0^\infty dz \frac{d\dot{N}^{\text{tde}}}{dz} \frac{1}{\chi^2(z)} \frac{1}{1+z} \left( \frac{dE}{df} \right)$$

Population of 1Msun stars disrupted by  $10^5 - 3 \times 10^5 - 4 \times 10^6 M_\odot$  (Broggi et al. 2024)

- two-body scattering
- number orbits per energy bin
- pericenter for total disruption

$$\frac{d\dot{N}}{dz} = \int d\epsilon \frac{d\dot{N}}{dz d\epsilon} = \int d\epsilon \frac{d\dot{N}}{d\epsilon} \frac{4\pi c \chi^2(z)}{H_0} \Phi(z) \quad \frac{dE}{df} = \sum_{i=1}^{N_{\text{orbs}}(\Delta\epsilon_j)} \left. \frac{dE}{df} \right|_i$$

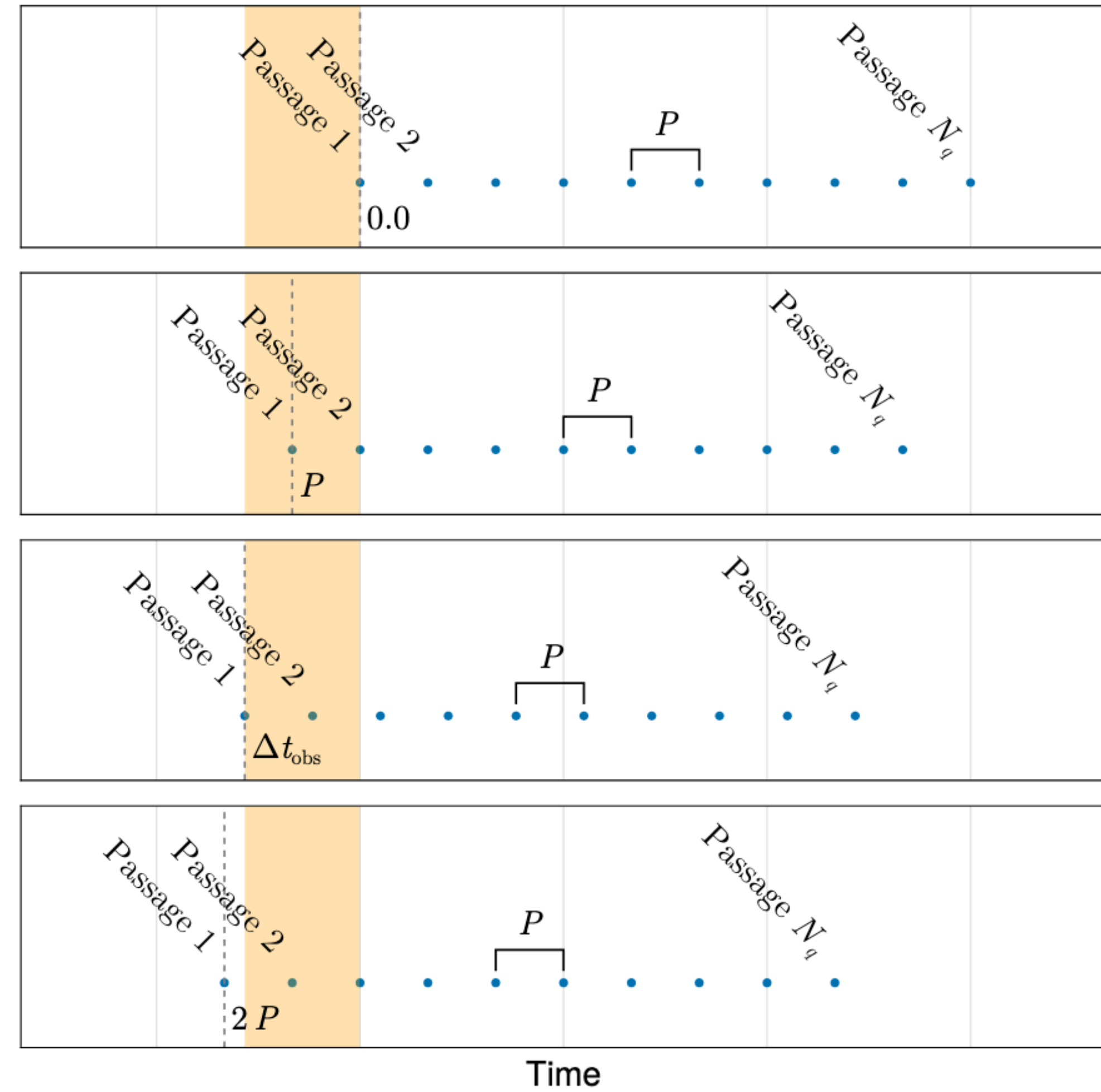
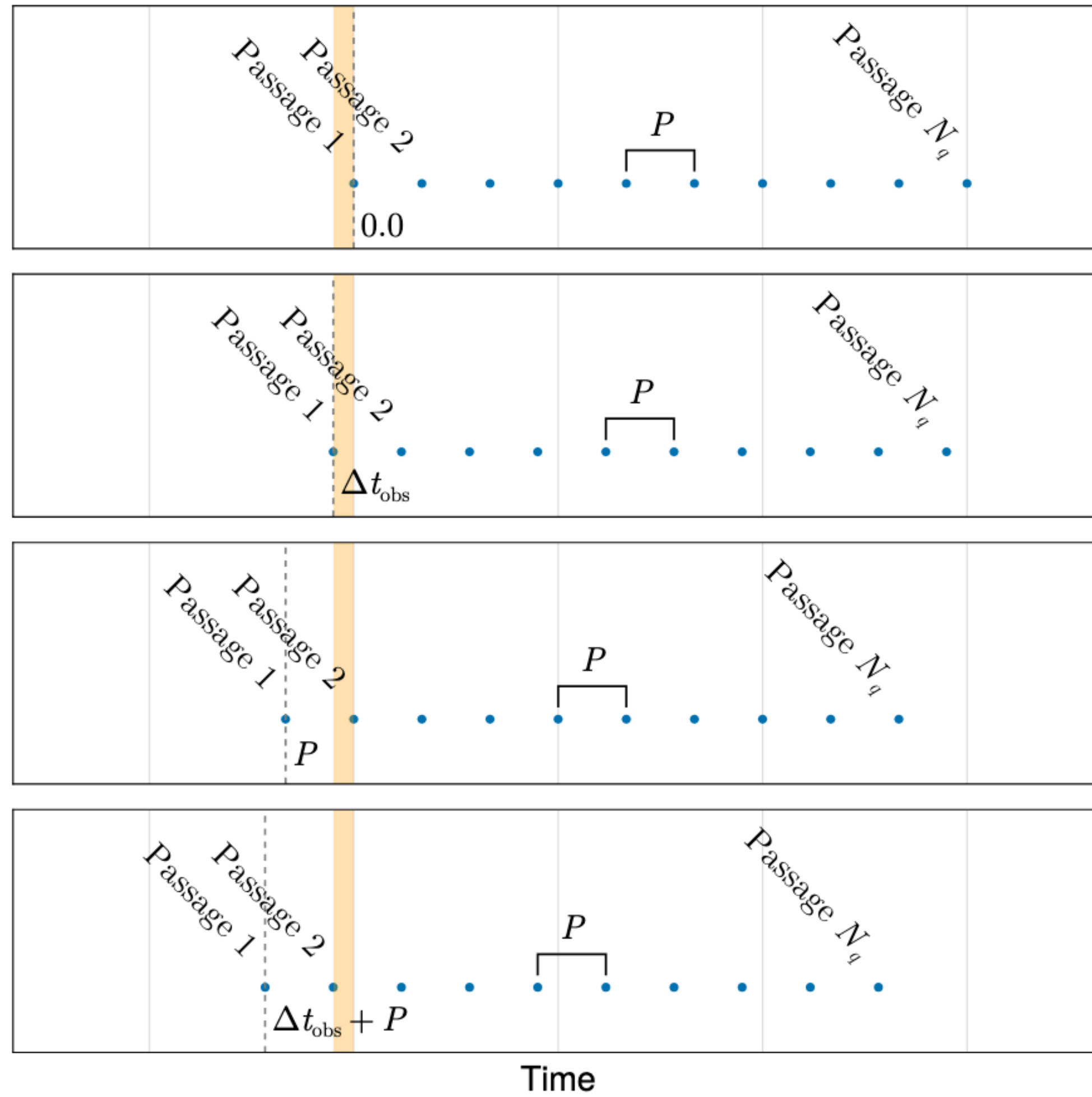
# rpTDEs: background



# rpTDEs: individual detections

$$P > \Delta t_{\text{obs}}$$

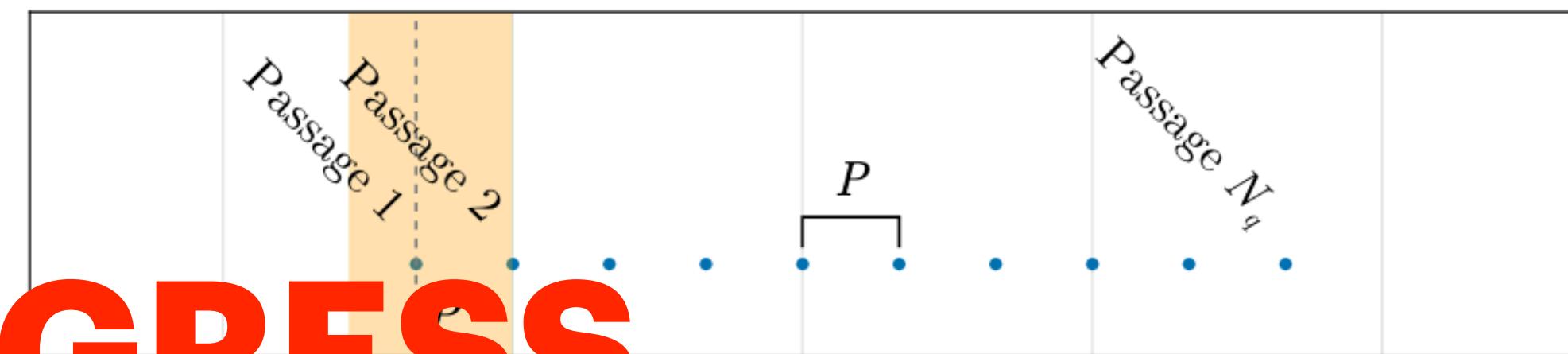
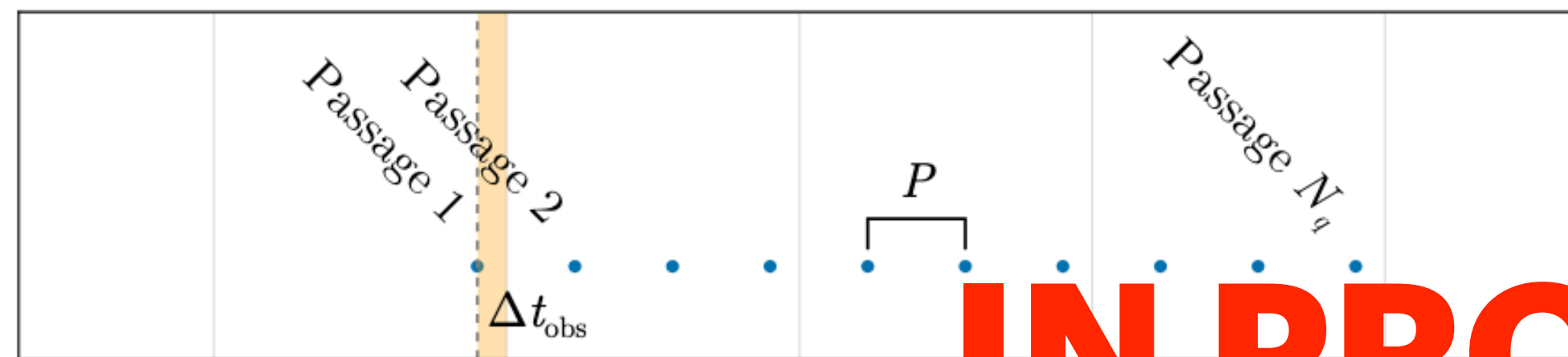
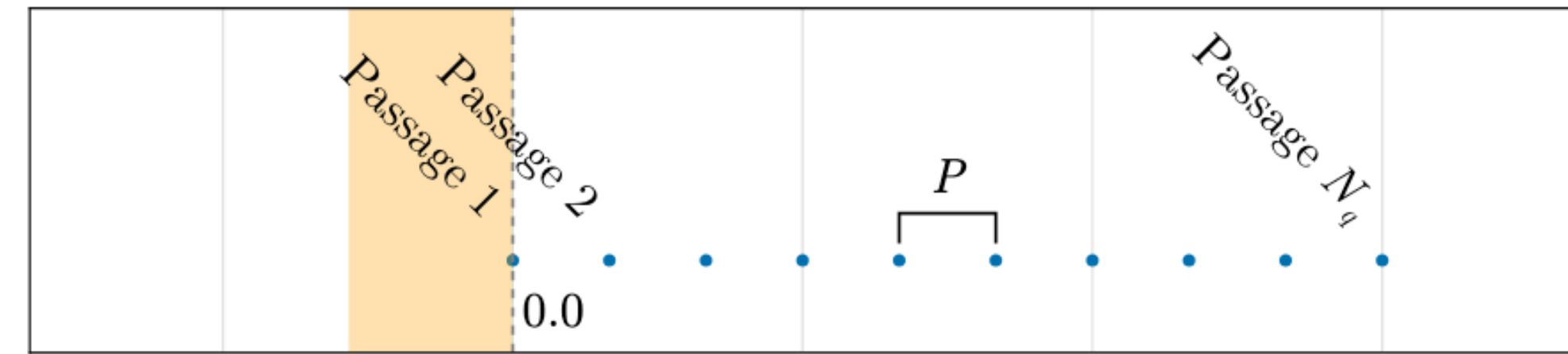
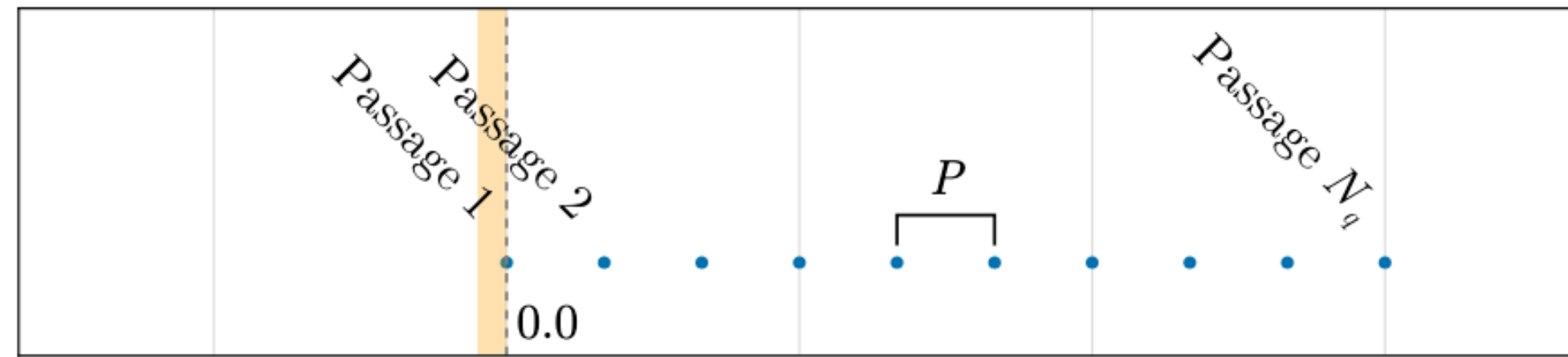
$$P < \Delta t_{\text{obs}}$$



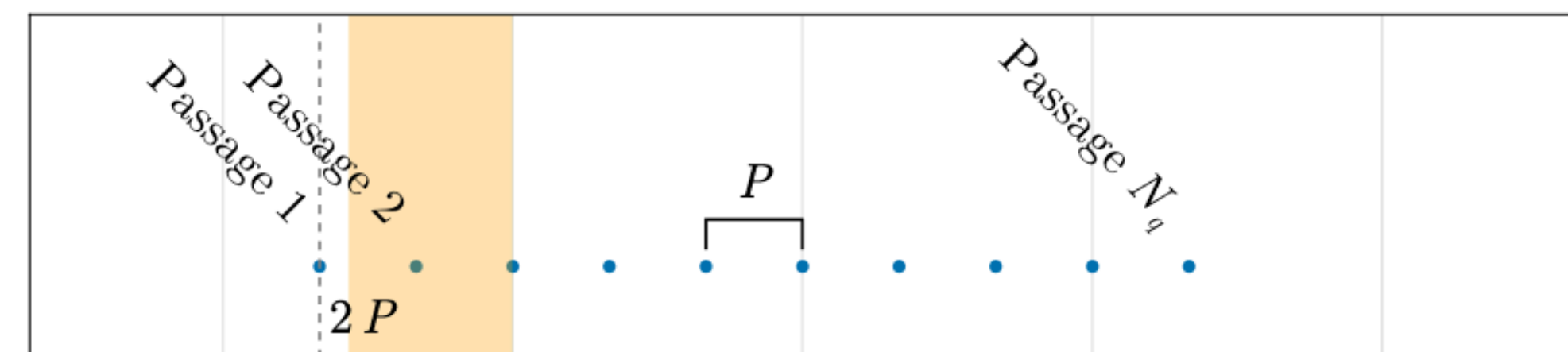
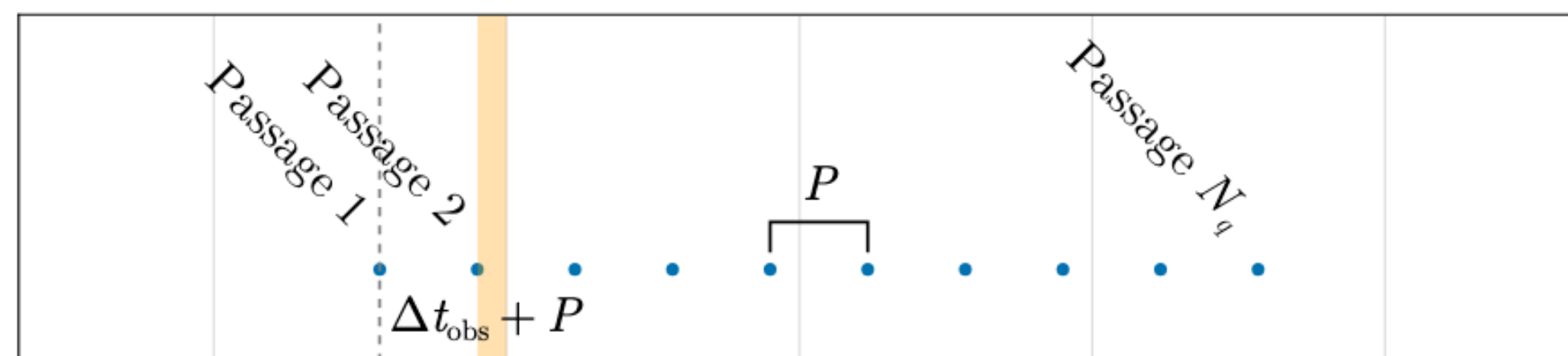
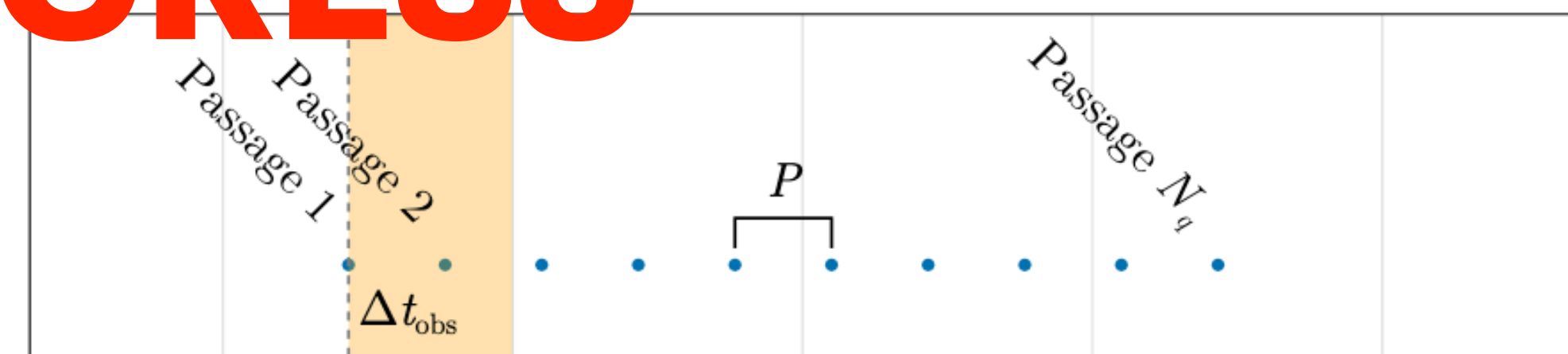
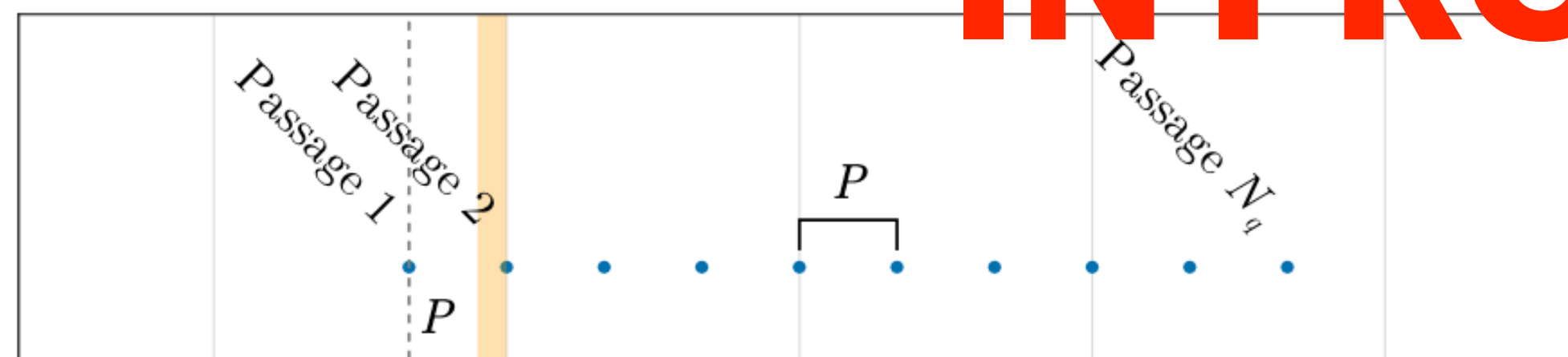
# rpTDEs: individual detections

$$P > \Delta t_{\text{obs}}$$

$$P < \Delta t_{\text{obs}}$$



**IN PROGRESS**



Time

Time

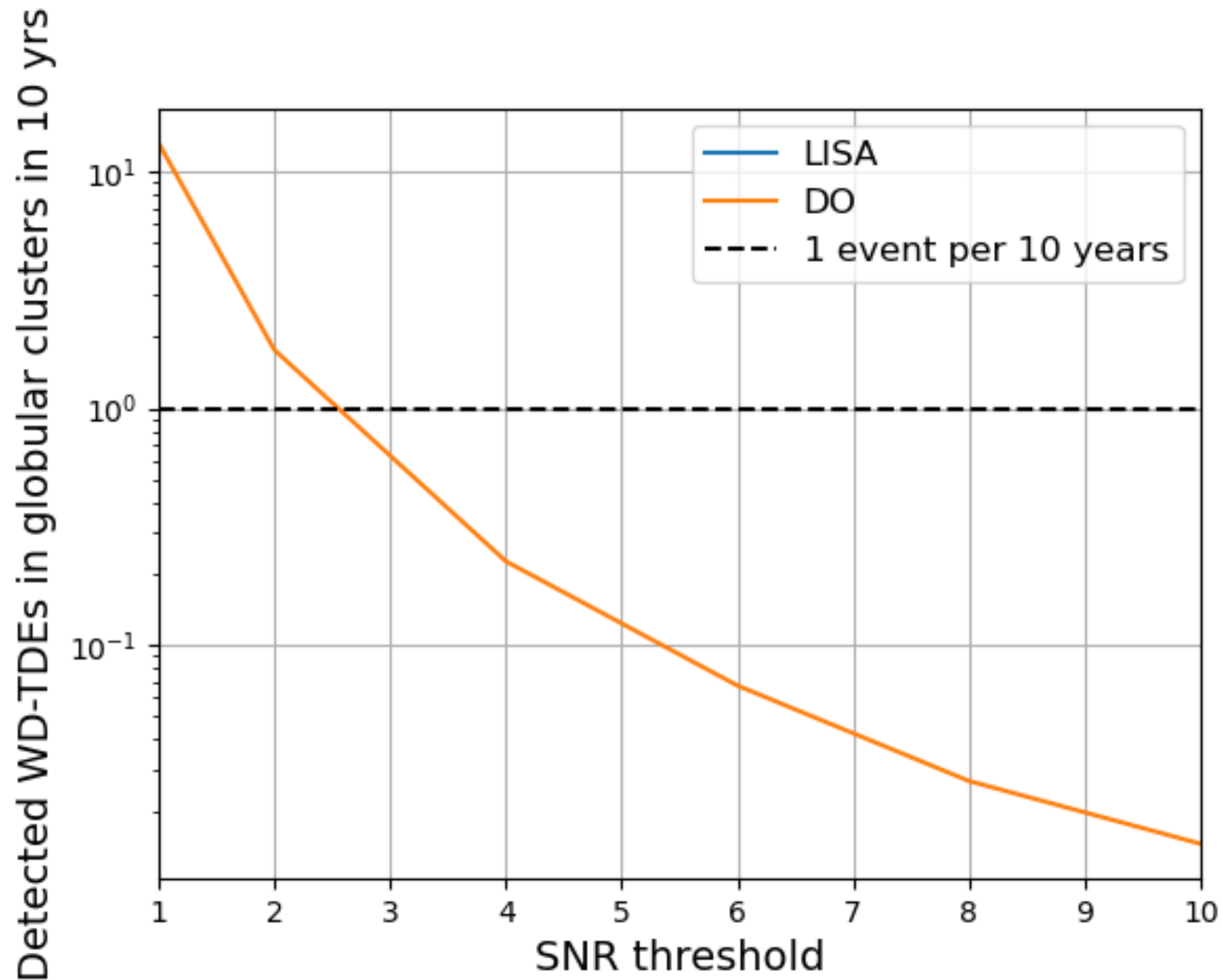
## Conclusions

- fTDEs very unlikely sources for LISA, but promising for DO
- rpTDE background can be a problem for detectors more sensitive at lower frequency
- rpTDEs could be individually detected? LISA? DO?

QUESTIONS?

## fTDEs: white dwarfs (II)

$$\frac{d^3 \dot{N}_{\text{det}}^{\text{fTDEs}}}{dz dM_{\bullet} dR_p} \approx \frac{d\Gamma(M_h)}{dR_p} \times N_{\text{gc}}(M_{\bullet}) \times \Phi(M_{\bullet}, z) \times \frac{4\pi\chi^2(z)}{H(z)} \times \Theta(z, M_{\bullet}, M_*, R_p)$$



$$N_{\text{gc}} \approx \left( \frac{M_{\bullet}}{4 \times 10^5 M_{\odot}} \right)$$

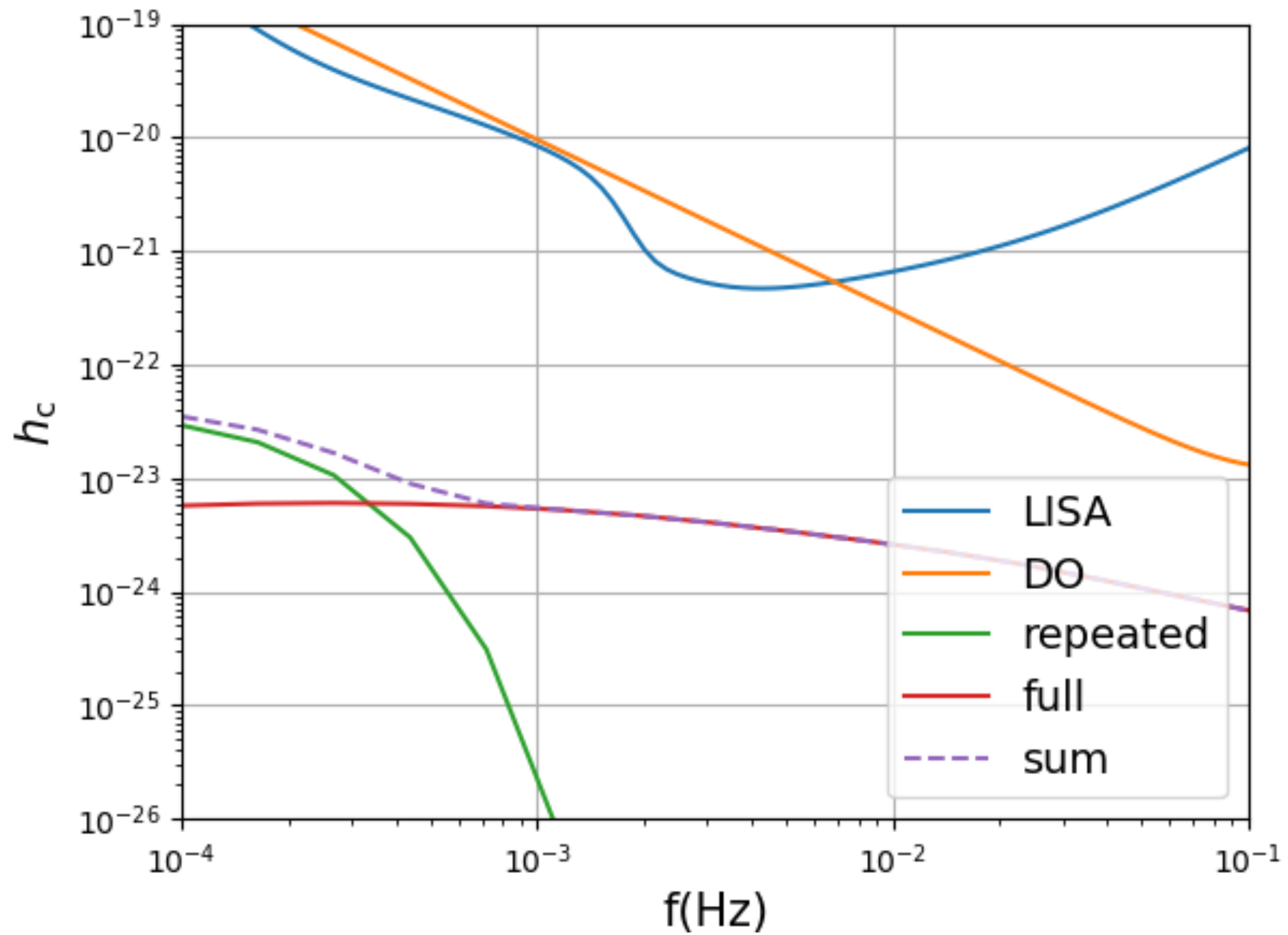
(Burkert & Tremaine10, Harris & Harris 11)

$$M_* = 0.5 M_{\odot}, M_h = 10^3 M_{\odot},$$

$$10^6 M_{\odot} \leq M_{\bullet} \leq 10^8 M_{\odot}$$



## Repeated TDEs + full TDEs



## Repeated TDEs

Empty loss cone

Individual detections

$$P < \Delta t_{\text{obs}}$$

$$\Delta t_{\text{obs}} = \tilde{n} P + p$$

$\tilde{n}$  : maximum number of subsequent passages