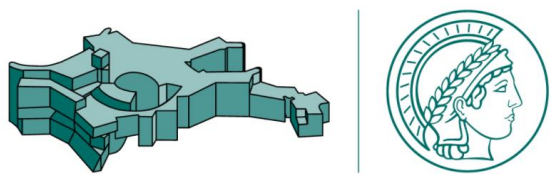


SMBH seeds and GWs from dense, low-metallicity star formation

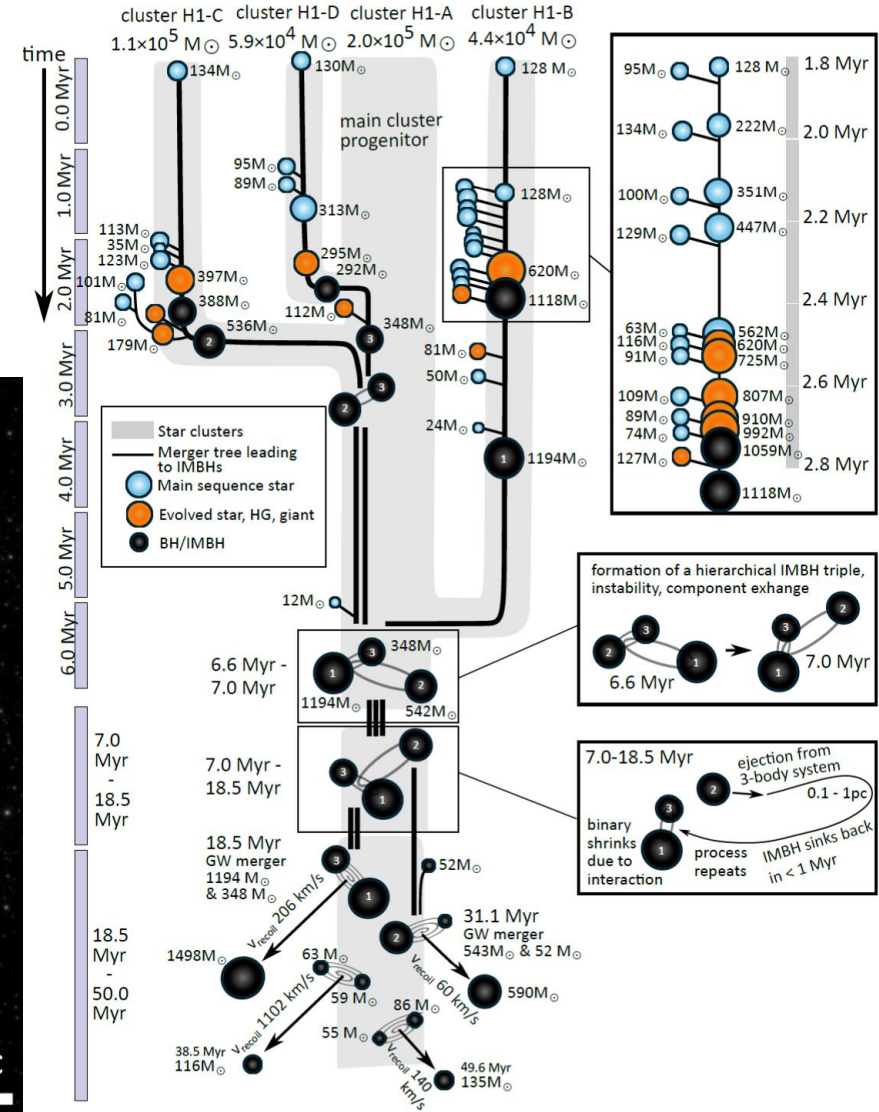
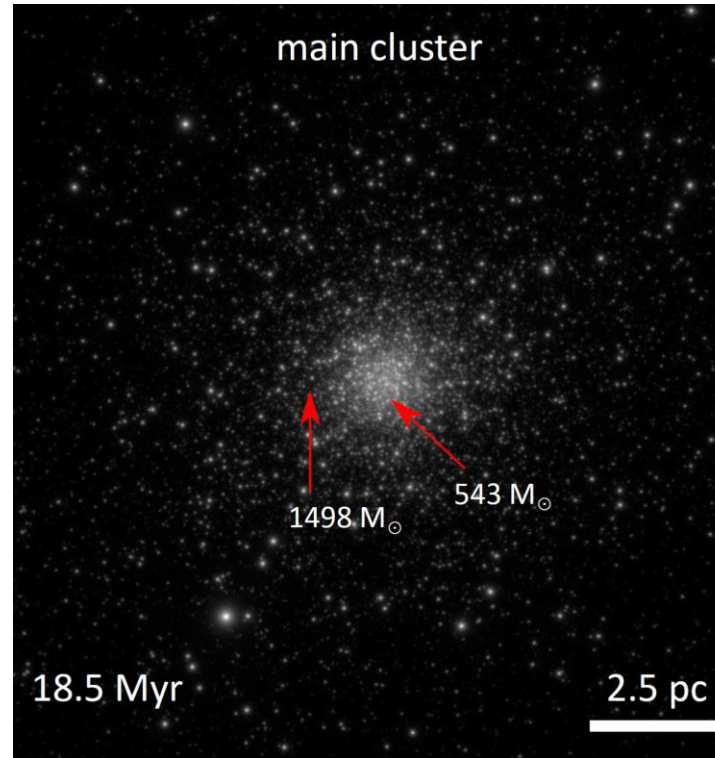
Antti Rantala

MPA Postdoctoral Fellow

Thorsten Naab, Natalia Lahén



MAX-PLANCK-INSTITUT
FÜR ASTROPHYSIK

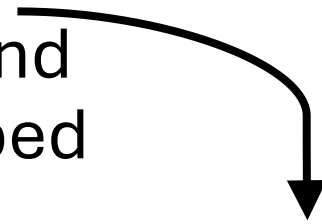


$$e^{\epsilon_H} = e^{\frac{1}{6} \epsilon_{USF}} e^{\frac{1}{2} \epsilon_{HS}} e^{\frac{1}{2} \epsilon_{HF}} e^{\frac{2}{3} \epsilon_{\tilde{U}_{SF}}} e^{\frac{1}{2} \epsilon_{HF}} e^{\frac{1}{2} \epsilon_{HS}} e^{\frac{1}{6} \epsilon_{USF}}$$

My work

- Modelling BHs of all masses in their stellar-dynamical environments...
- ... with novel integrators and HPC codes I have developed

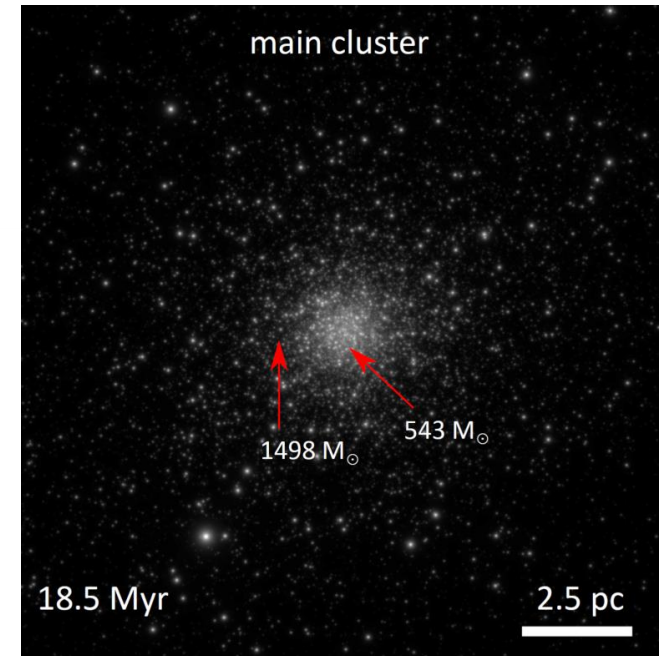
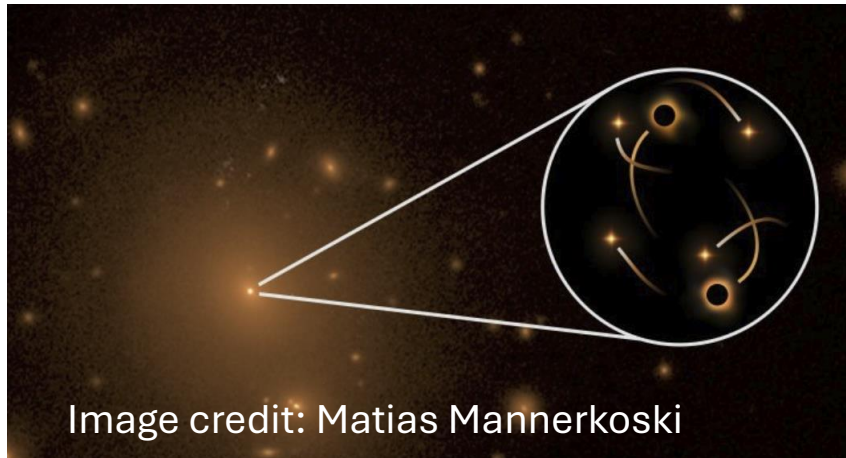
KETJU



BIFROST

- Galaxies and their supermassive black holes (SMBHs)
- **public** dynamics library → Peter Johansson's group homepage
- talks by Alex Rawlings and Atte Keitaanranta, Nianyi Chen

- Massive star clusters including collisional SMBH seed formation



My work

- Modelling BHs of all masses in their stellar-dynamical environments...
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KETJU



- Galaxies and their supermassive black holes (SMBHs)
- public dynamics library
- (talks by Alex Rawlings and Atte Keitaanranta, Nianyi Chen)

BIFROST



- Massive star clusters including collisional SMBH seed formation

An one-slide first look after the main talk: the new faster KETJU

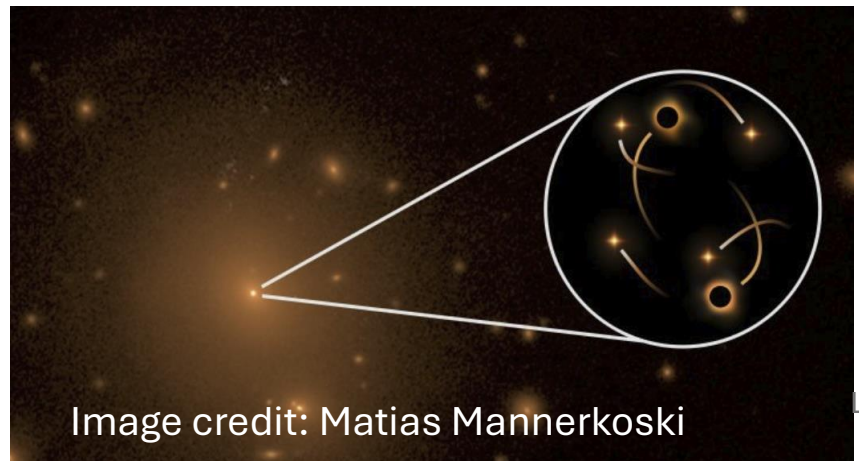
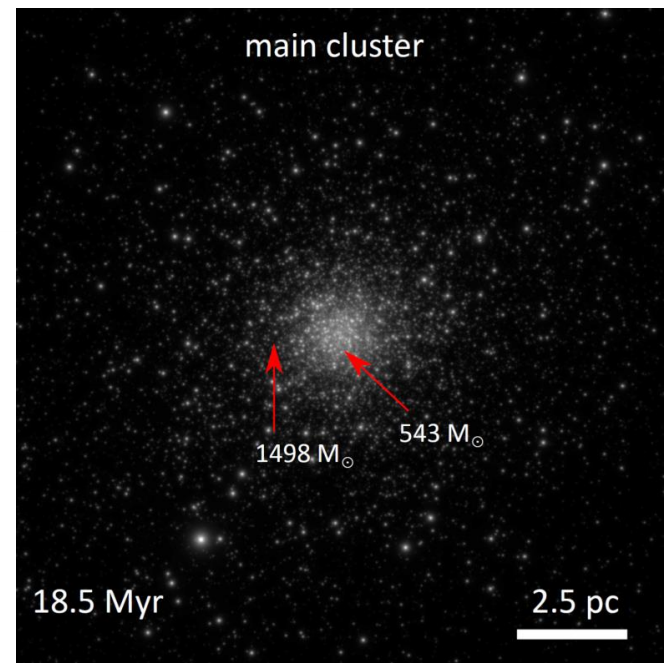
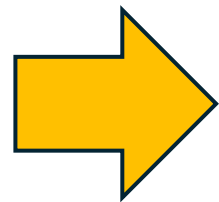
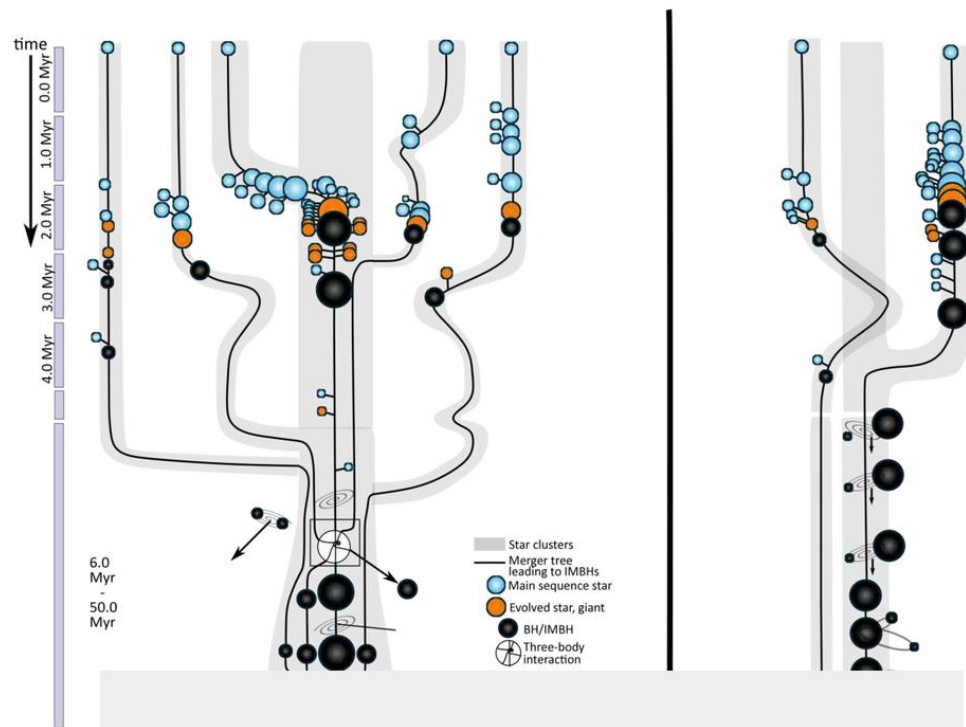


Image credit: Matias Mannerkoski

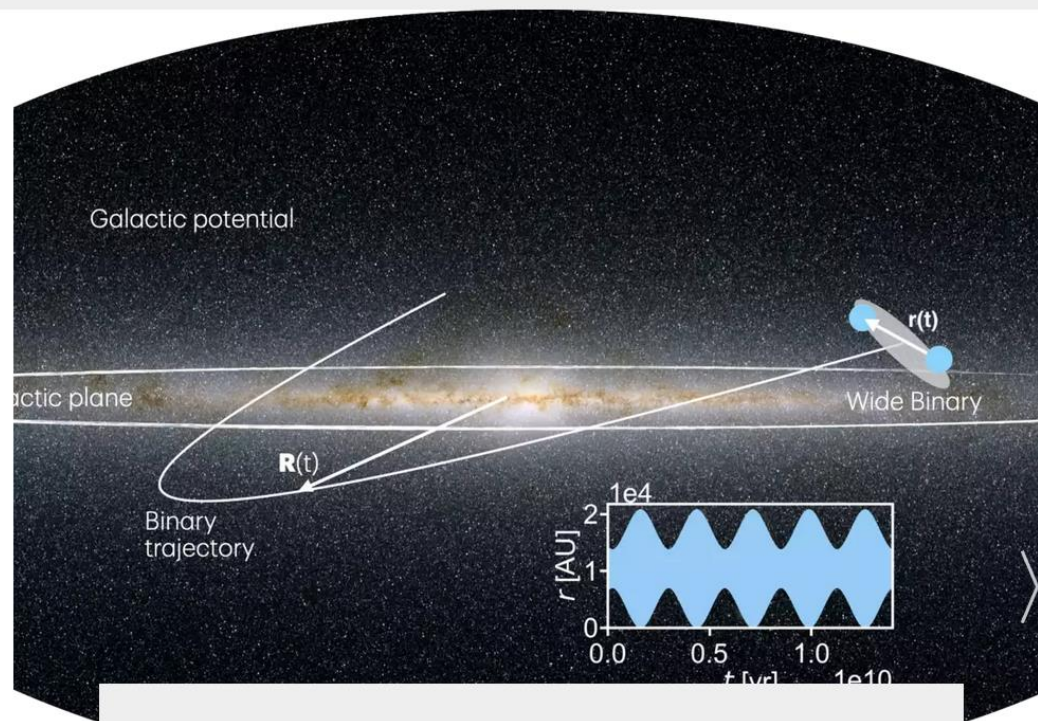


18.5 Myr

2.5 pc



Rapidly merging stars and black holes



How galaxies make black holes collide

Jakob's galactic binaries

MPA homepage highlight this month

The SMBH seed origin puzzle

Proposed
SMBH seeding
mechanisms

Directly collapsing
gas clouds

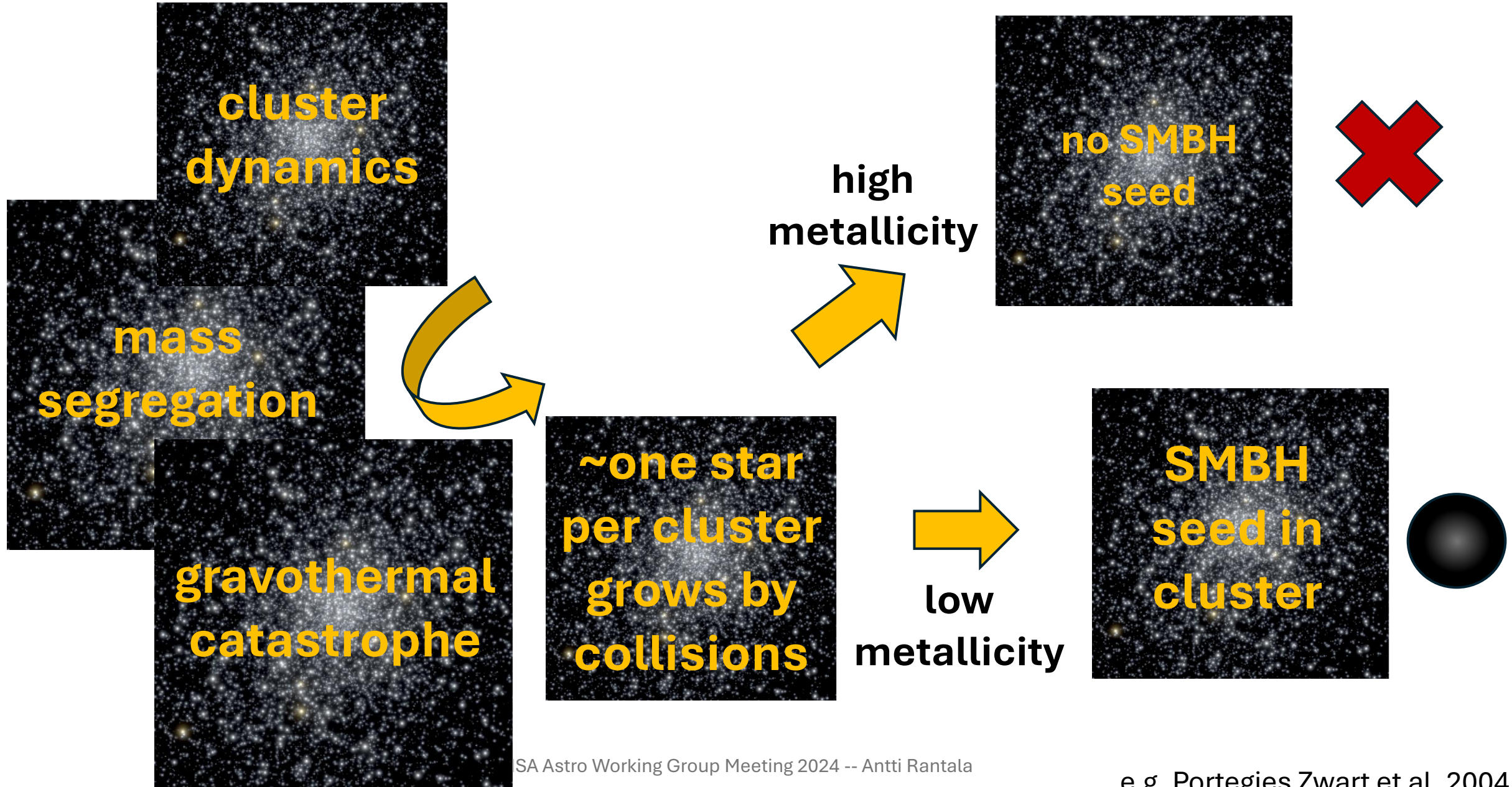
Runaway stellar
collisions

Stellar remnants

Exotic “new”
physics

*Natural
consequence* of
clustered,
dense, low-
metallicity star
formation in the
early Universe?

SMBH seeds from runaway stellar collisions



Simulating the runaway channel – isolated clusters

Portegies Zwart et al. 1999;
Portegies Zwart & McMillan 2002;
Gürkan et al. 2004;
Portegies Zwart et al. 2004;
Freitag et al. 2006a,b;
Baumgardt & Klessen 2011;
Mapelli 2016;
Rodriguez+19;
Rizzuto et al. 2021, 2022;
Vergara et al. 2023, 2024 ;
Arca Sedda et al. 2023a,c,b;
Prieto et al. 2024;

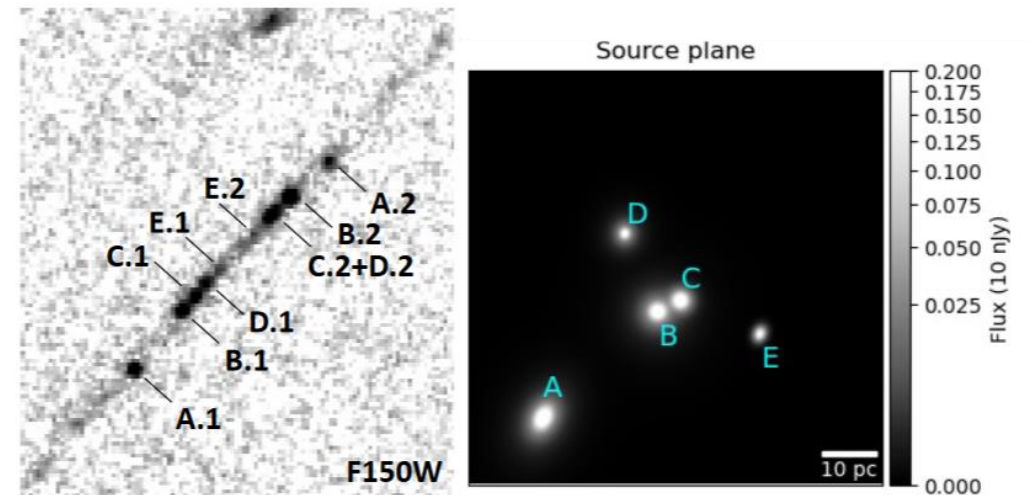
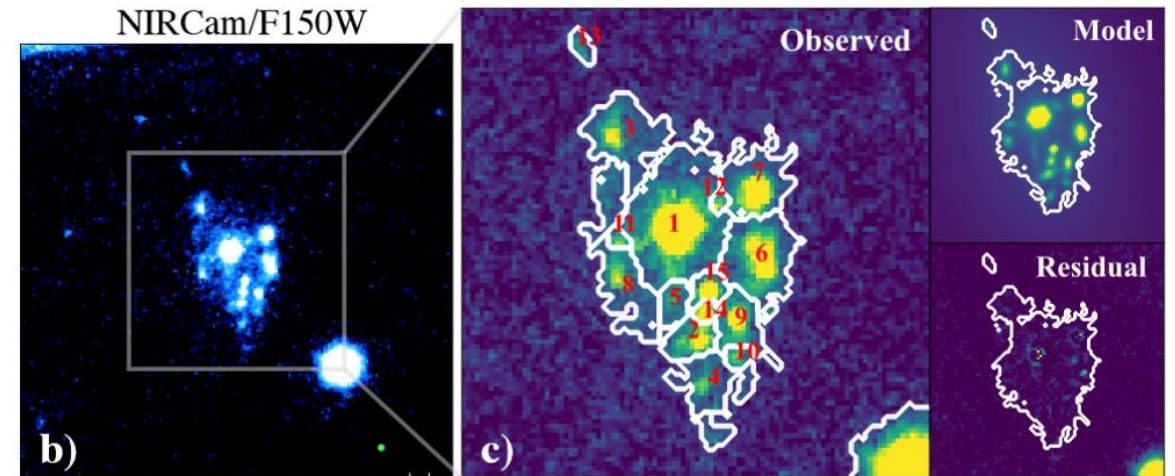


but do young, dense, low-
metallicity star clusters
look like this?

Massive star cluster formation regions at high z

Fujimoto+24

- recent JWST observations reveal clumpy, clustered star formation at high z
- **the Cosmic Grapes** at $z=6$ (Fujimoto+24)
- **the Cosmic Gems arc**: five close parsec-size young star clusters at $z=10.2$ with masses of $M \sim 10^6 M_{\odot}$ in (Adamo+24)
- **early MW history** was clumpy (Belokurov & Kravtsov 2023)
- **hydrodynamical simulations** of massive star cluster formation in low-metallicity dwarf starbursts **support this view** (Lahén+20,24)



Adamo+24

What are the consequences of the hierarchical star cluster assembly for the collisional runaway scenario?

The modern direct N-body simulation code *BIFROST*

Rantala, Naab, Springel (2021)

Rantala et al. (2023)

Rizzuto, Naab, Rantala et al. (2023)

Rantala & Naab 2024a

Rantala, Naab & Lahén 2024b

Rantala 2024d in prep.

Souvaitzis, Rantala, Naab in prep.

4th order forward direct summation code *BIFROST*

Hierarchical 4th order forward symplectic integrator

Direct summation, GPU acceleration

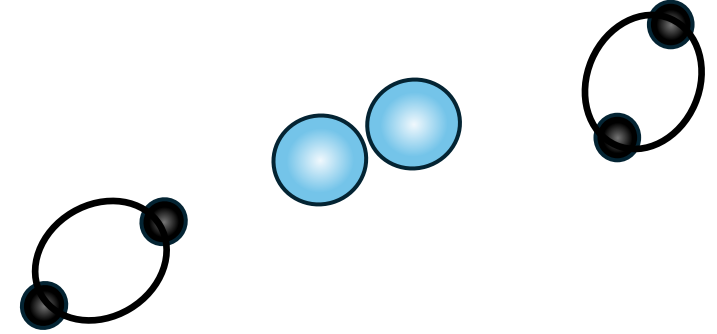
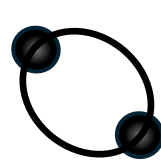
$$e^{\epsilon \mathbf{H}} = e^{\frac{1}{6} \epsilon \mathbf{U}_{\text{SF}}} e^{\frac{1}{2} \epsilon \mathbf{H}_{\text{S}}} e^{\frac{1}{2} \epsilon \mathbf{H}_{\text{F}}} e^{\frac{2}{3} \epsilon \tilde{\mathbf{U}}_{\text{SF}}} e^{\frac{1}{2} \epsilon \mathbf{H}_{\text{F}}} e^{\frac{1}{2} \epsilon \mathbf{H}_{\text{S}}} e^{\frac{1}{6} \epsilon \mathbf{U}_{\text{SF}}}$$

4th order forward direct summation code *BIFROST*

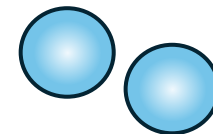
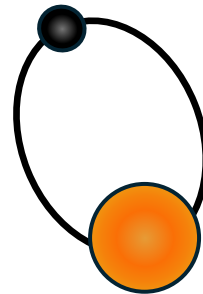
Hierarchical 4th order forward symplectic integrator

Secular and regularized integration of few-body systems incl. post-Newtonian terms

Efficient parallelization (MPI shared memory): arbitrary binary fractions up to 100% supported



Roughly similar approach as in KETJU: MSTAR-like integrator (Rantala+20) + slow-down algorithm (Mikkola+96, Wang+20)

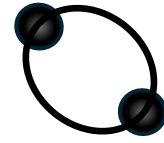


4th order forward direct summation code *BIFROST*

Hierarchical 4th order forward symplectic integrator

Secular and regularized integration of few-body systems incl. post-Newtonian terms

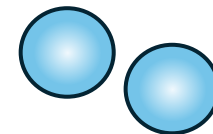
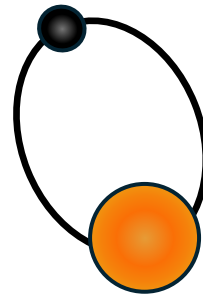
Rapid single & binary stellar population synthesis code SEVN (Iorio+23)



BH-BH mergers using fitting formulas to numerical relativity

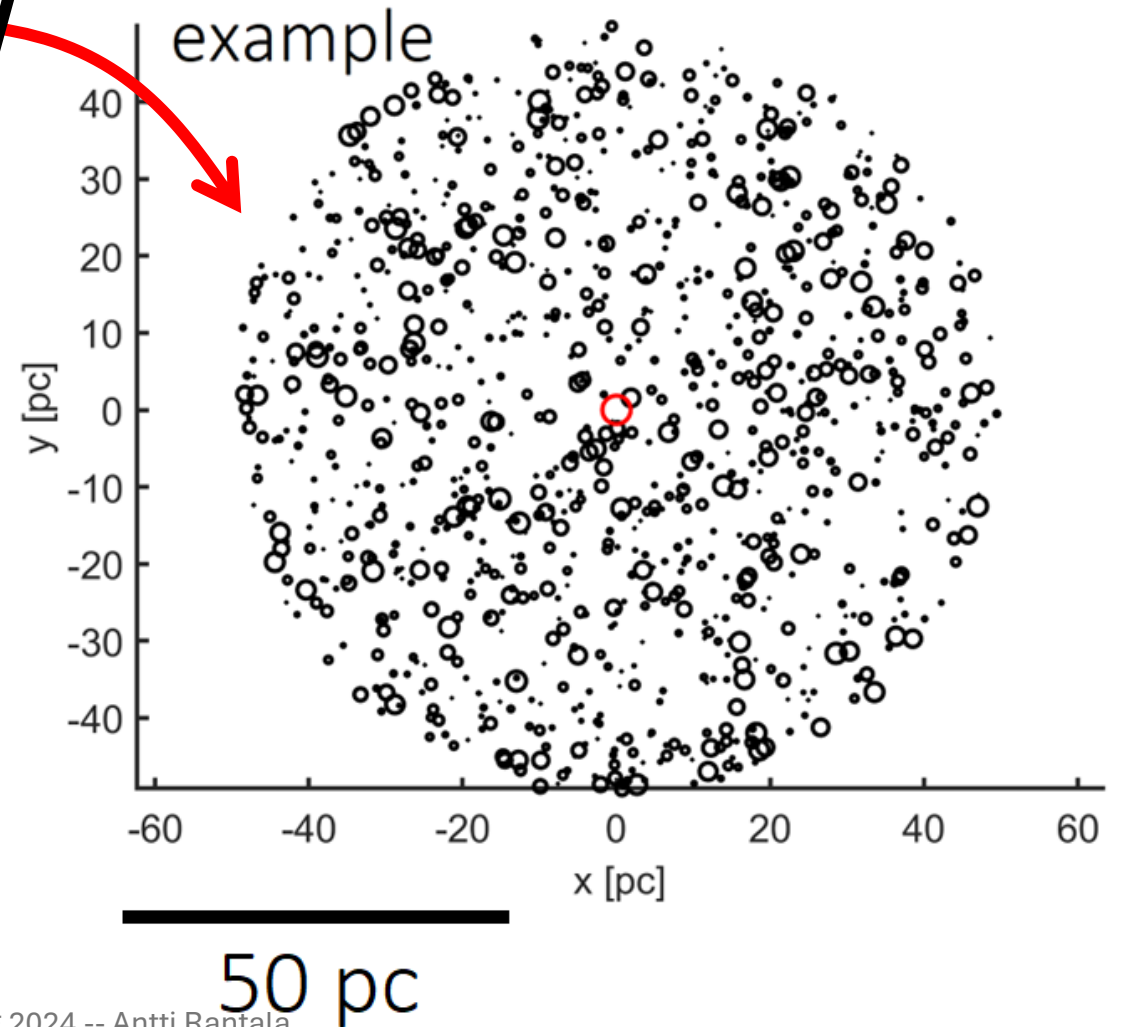
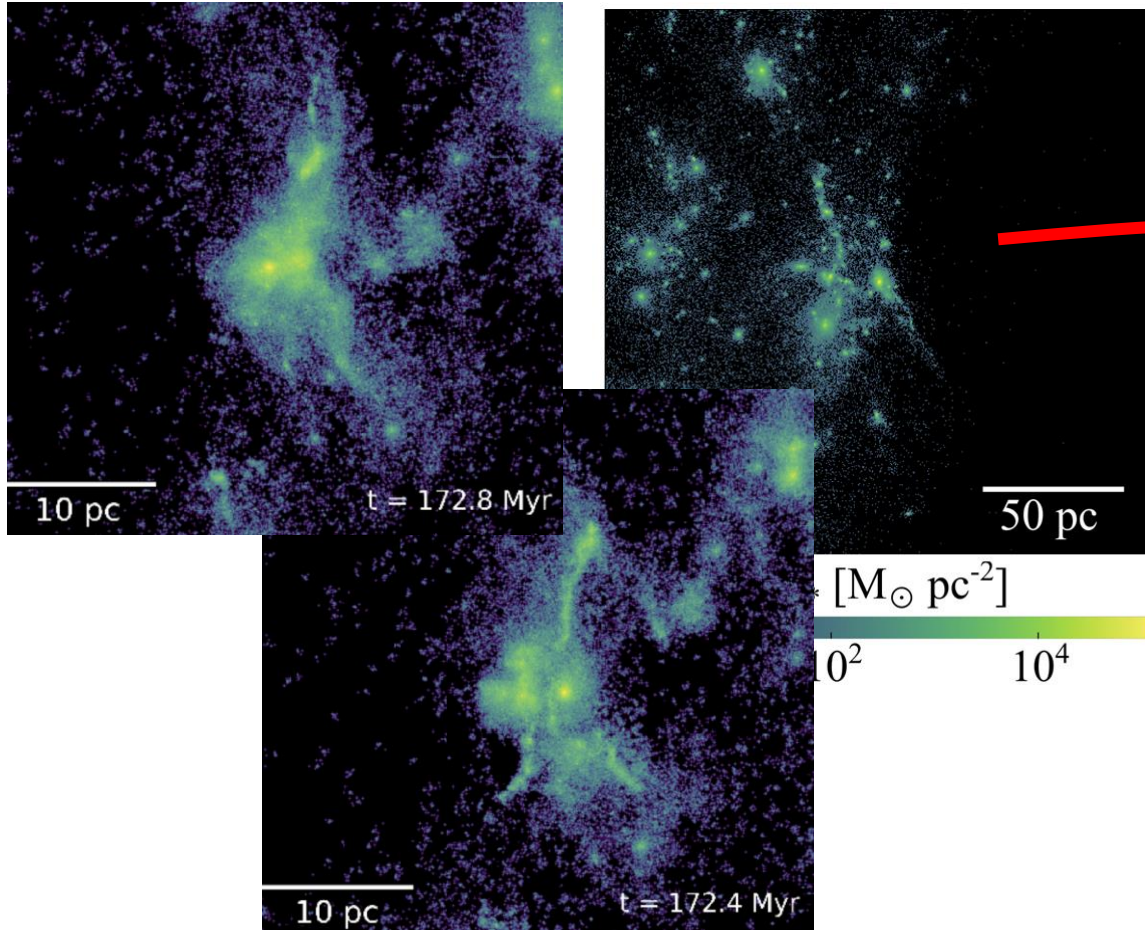


Prescriptions for tidal disruption events and stellar mergers



Lahén+2020, 2024 the **GRIFFIN** project

Initial conditions for the N-body
FROST-CLUSTERS project
(Rantala+24b)

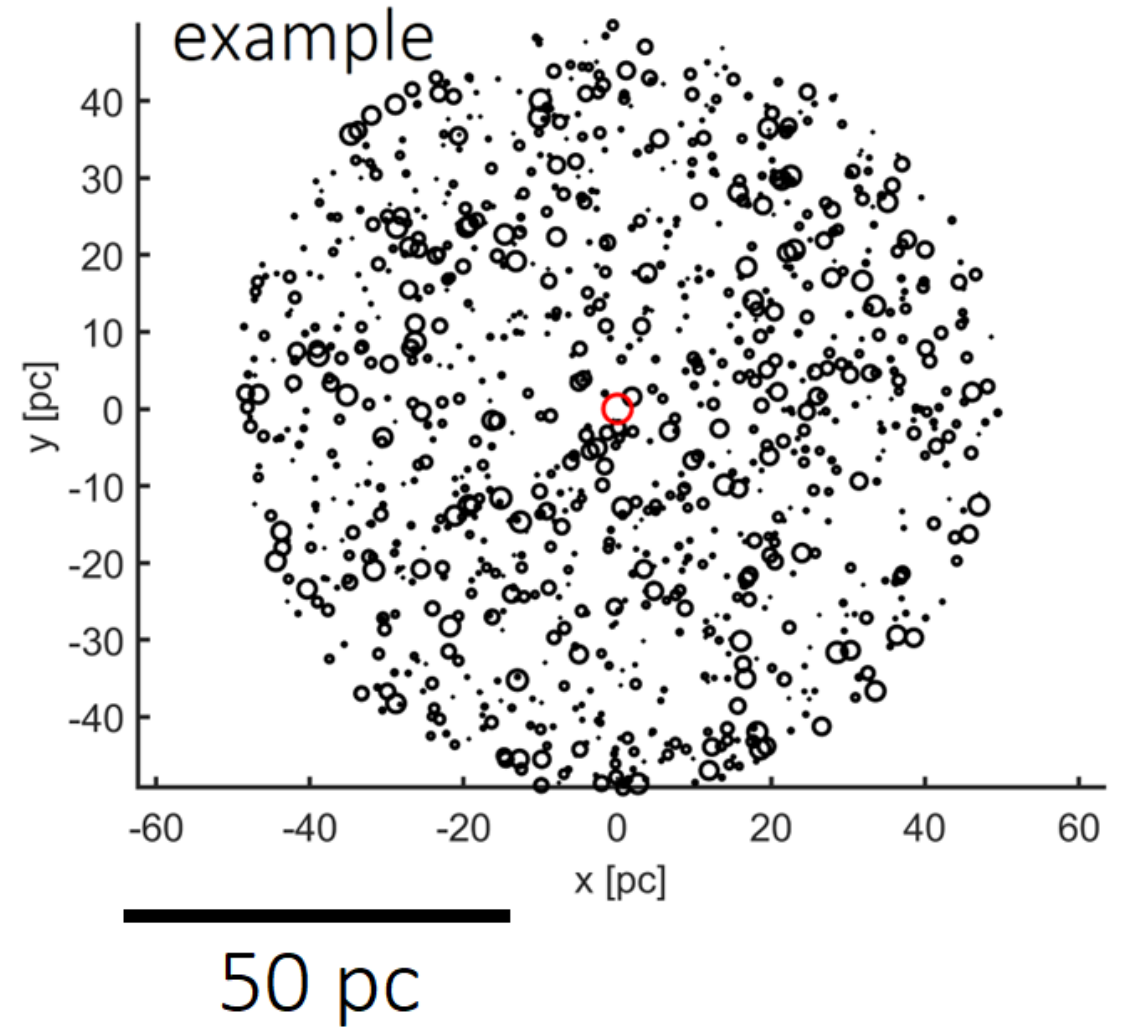


star-by-star star cluster formation
simulations in a full hydrodynamical
dwarf galaxy setting

Simulation setup

Key model ingredients:

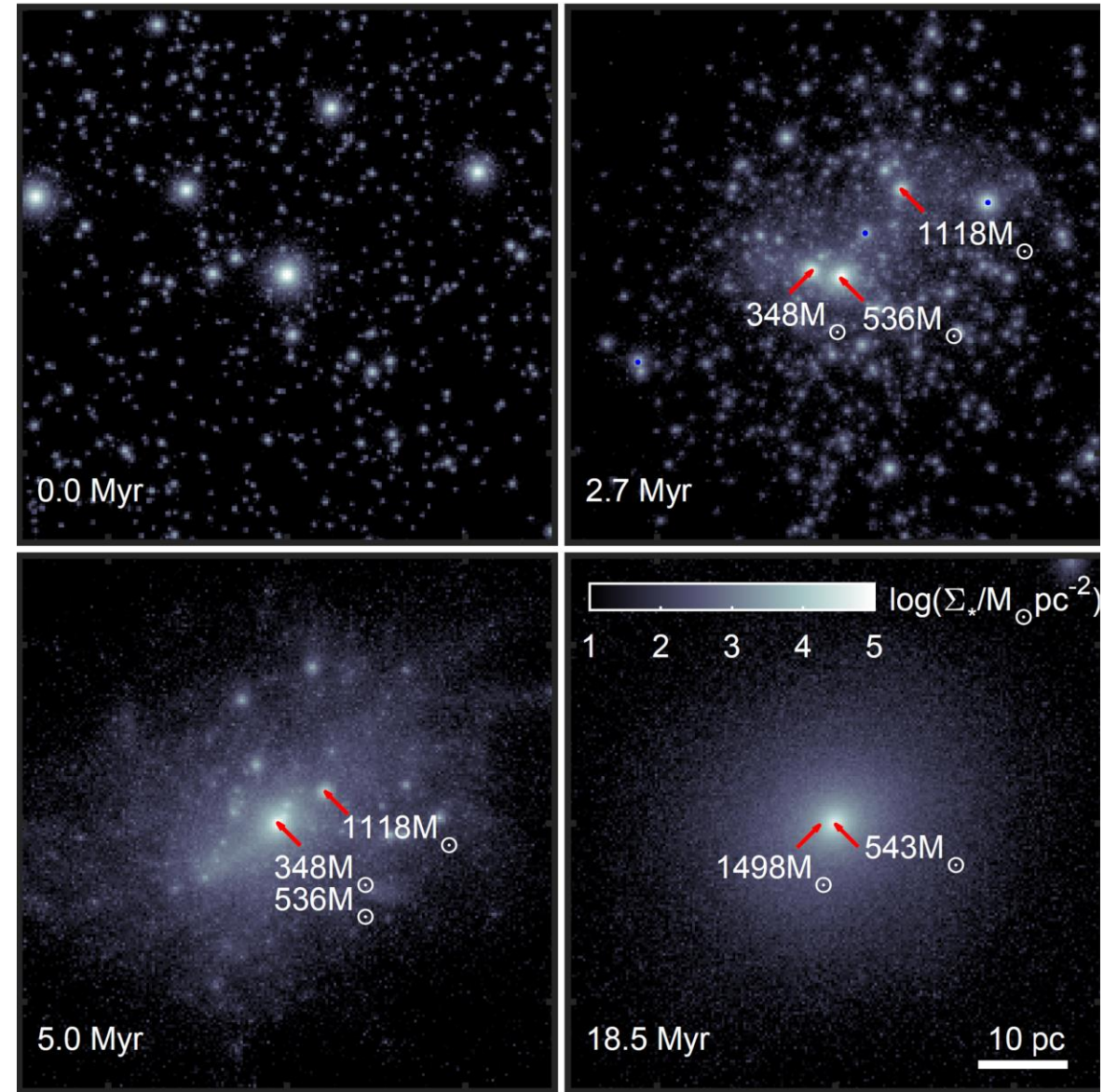
- Universal cluster mass function (slope -2)
- Shallow star cluster mass-size relation with small birth radii
- metallicity $Z = 0.01$ of solar



Simulation setup

Key model ingredients:

- Universal cluster mass function (slope -2)
- Shallow star cluster mass-size relation with small birth radii
- metallicity $Z = 0.01$ of solar
- **$N \sim 2.4$ million stars** in ~ 1000 star clusters between $\sim 100 M_{\odot}$ and $2.5 \times 10^5 M_{\odot}$
- converging radial flow of -3.5 km/s and similar random component
- central cluster densities $\sim 10^6 M_{\odot} \text{ pc}^{-3}$
- single-star Kroupa IMF up to $150 M_{\odot}$ with Yan&Kroupa (2023) m_{max} limit for low-mass star clusters



Simulation setup

Key model ingredients:

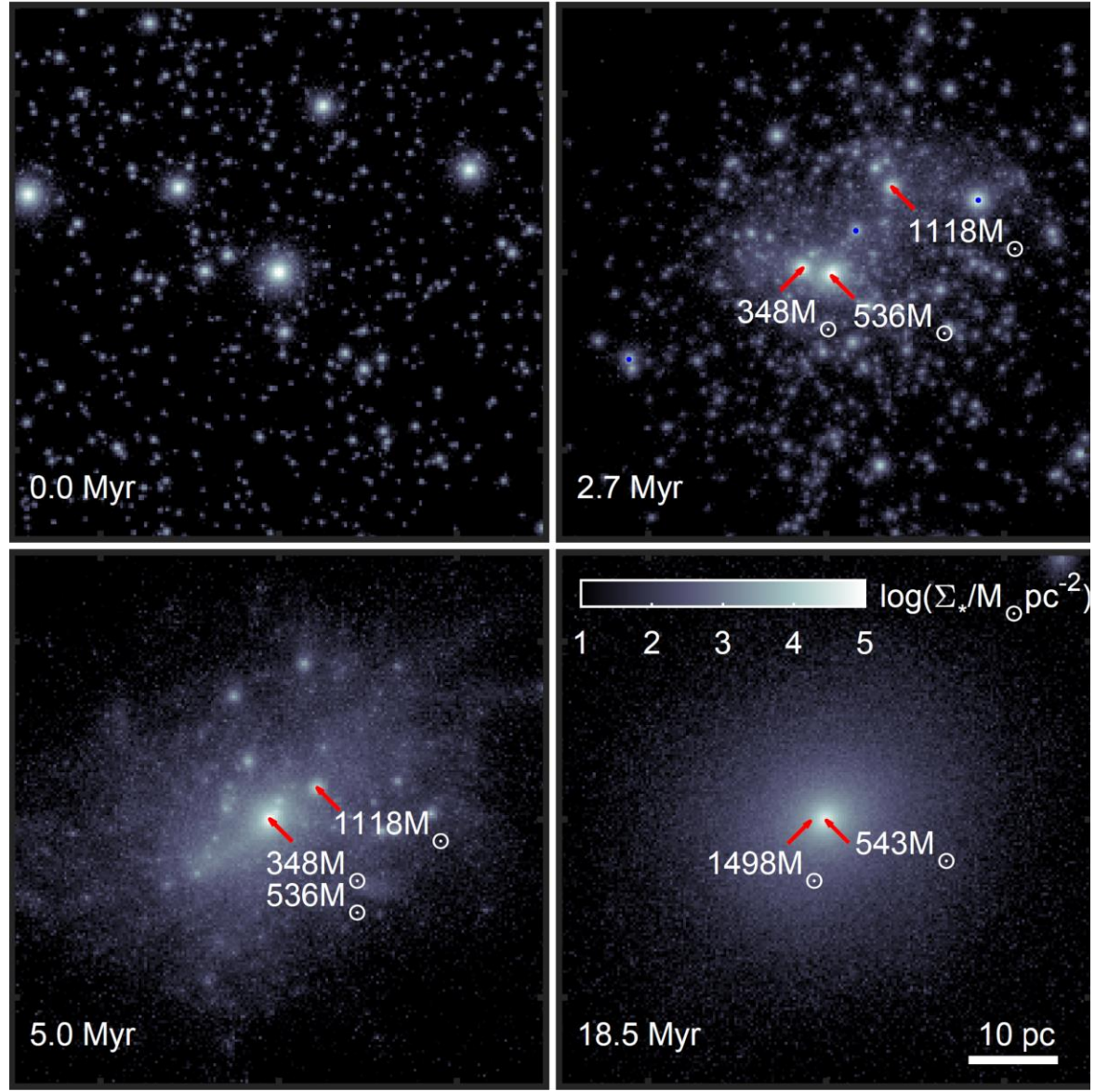
Simulations so far:

~1/3 runs with single stars (mmax = 150 Msun or 450 Msun)

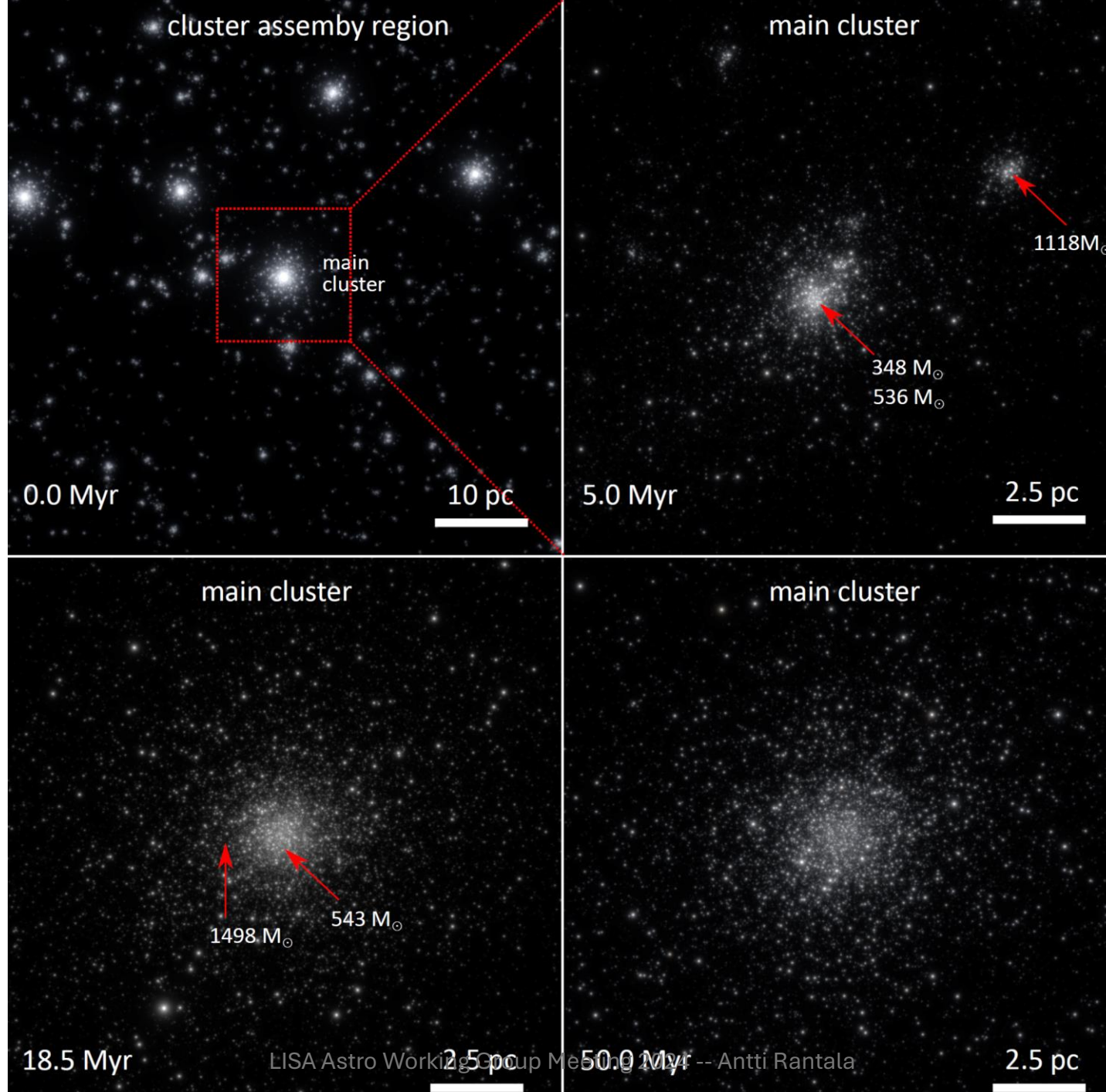
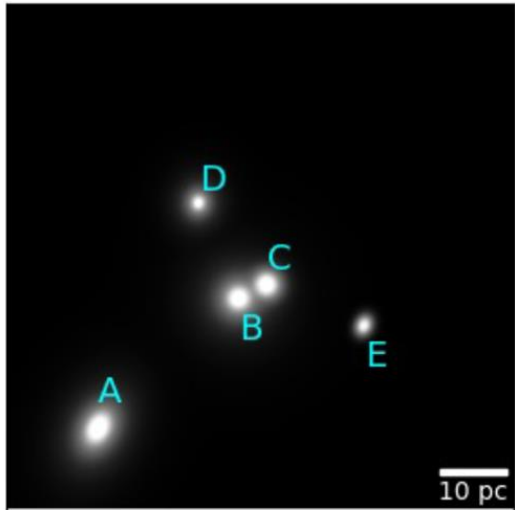
~ 1/3 of runs with primordial **binaries**

~ 1/3 runs with primordial **triples**

→ up to 800k stars in binaries and triples in the simulations

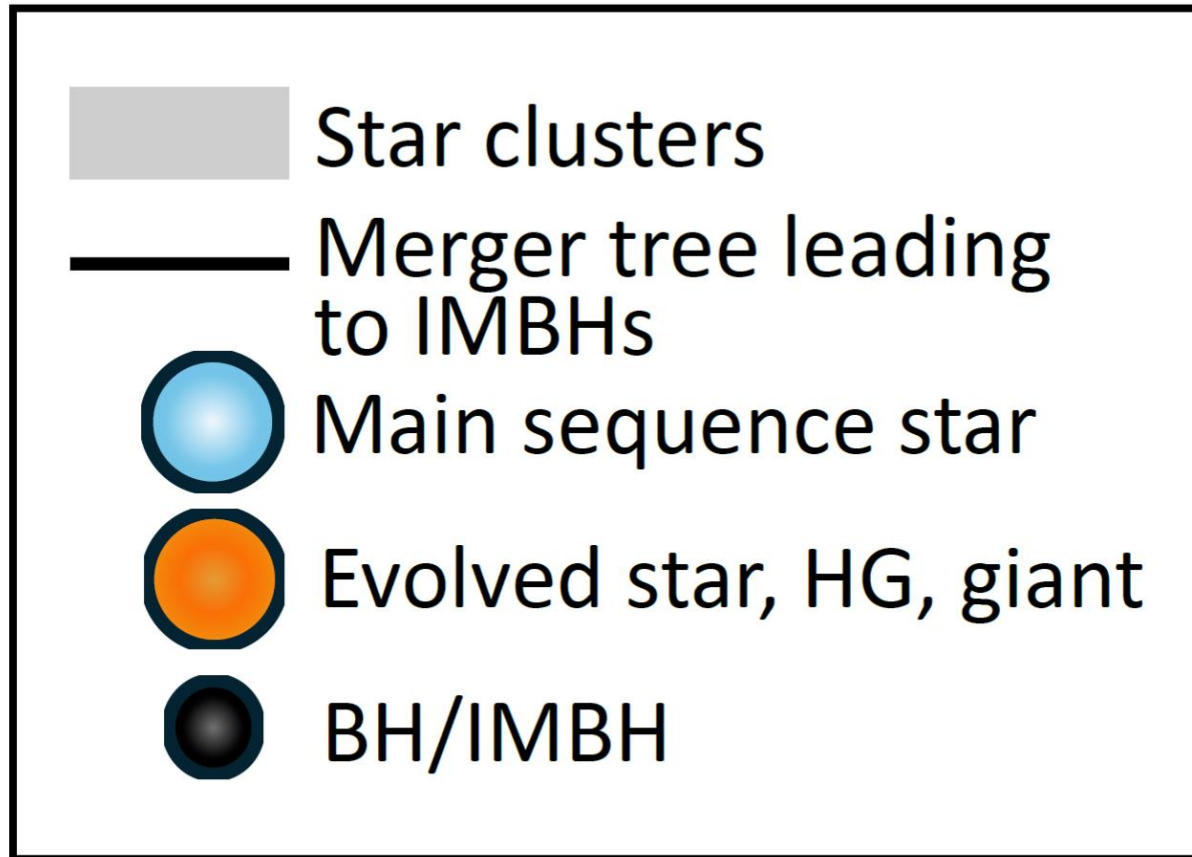


Hierarchical assembly on a 10 Myr time-scale

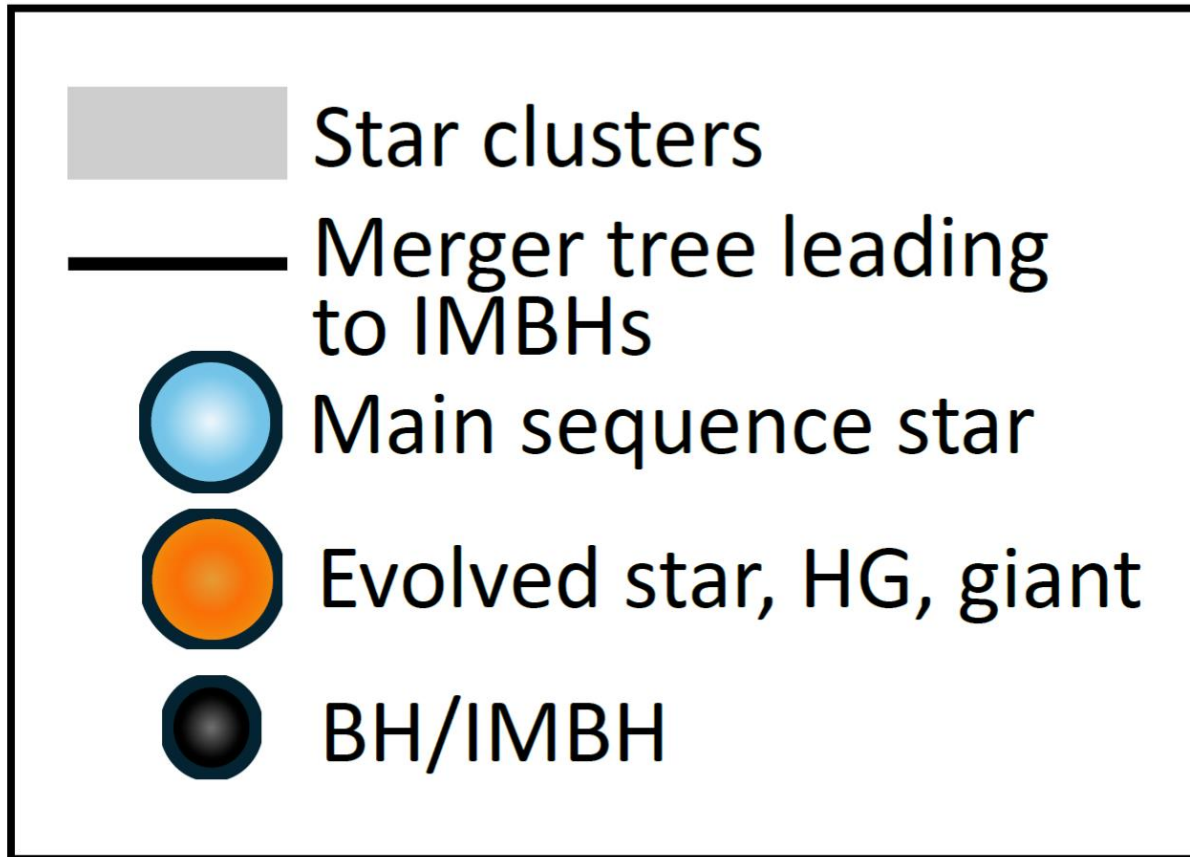


FROST-CLUSTERS I
mock BVR view
MYOSOTIS code by
Khorrami+19

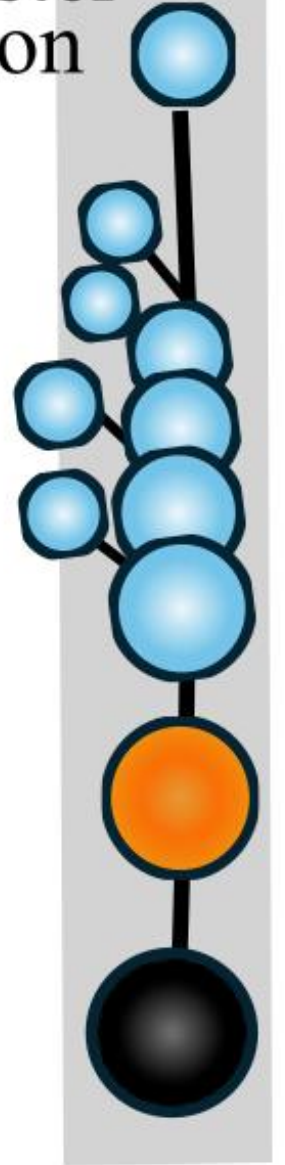
Star cluster and SMBH seed progenitor star merger trees



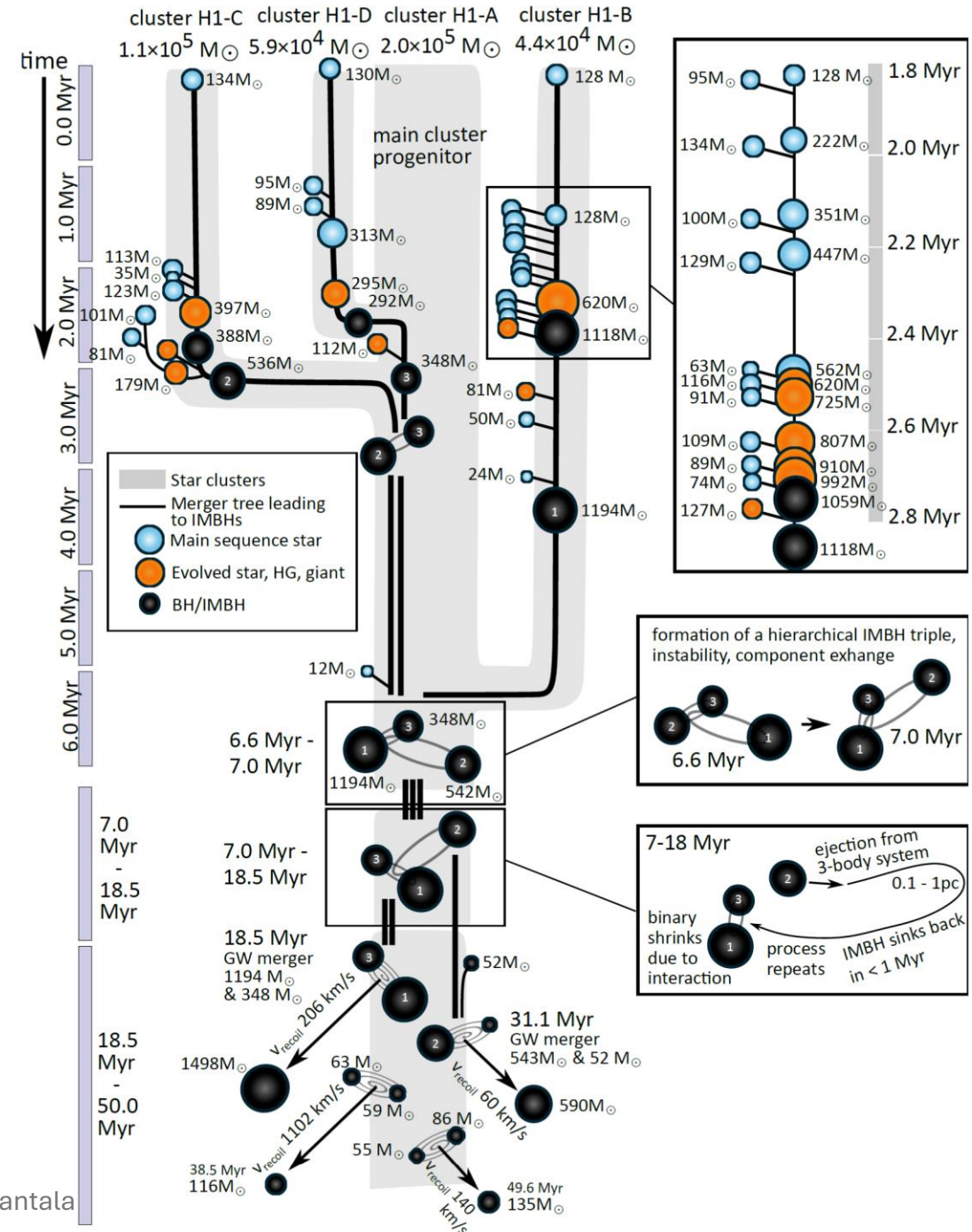
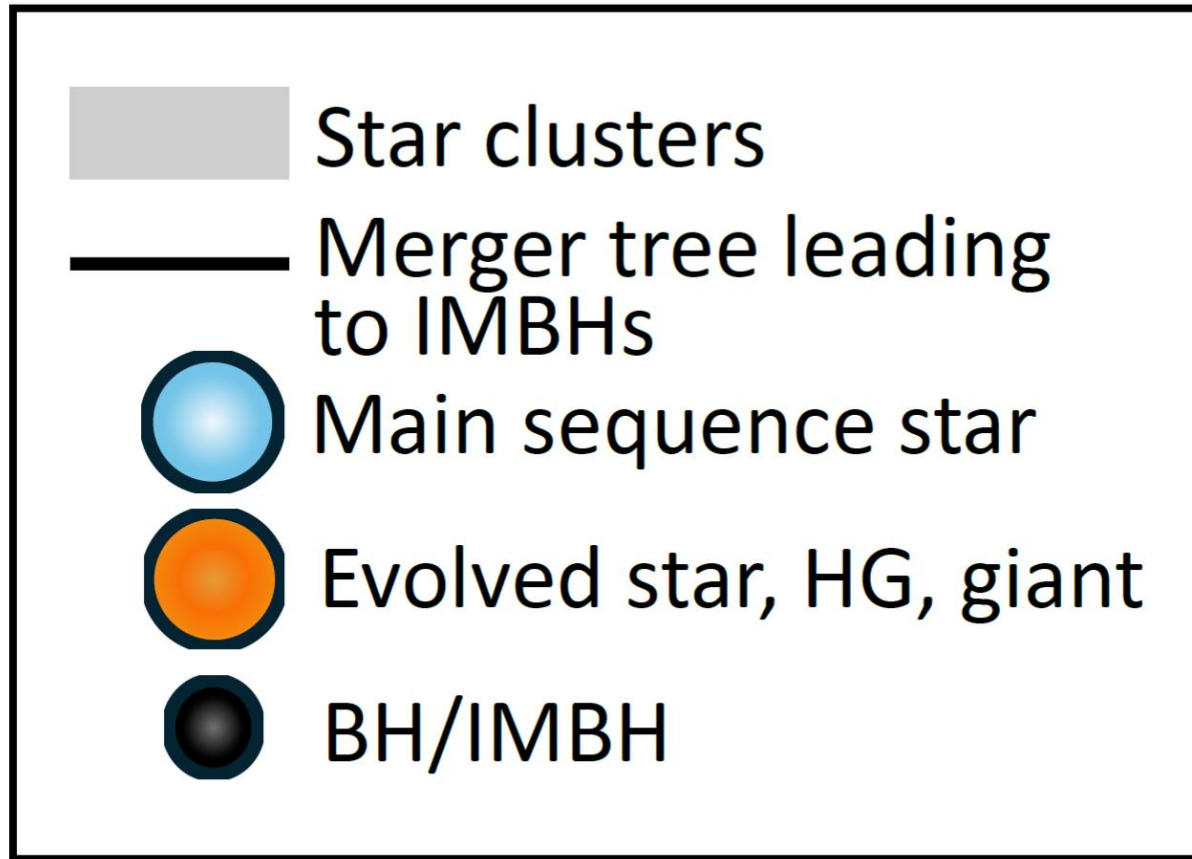
Star cluster and SMBH seed progenitor star merger trees



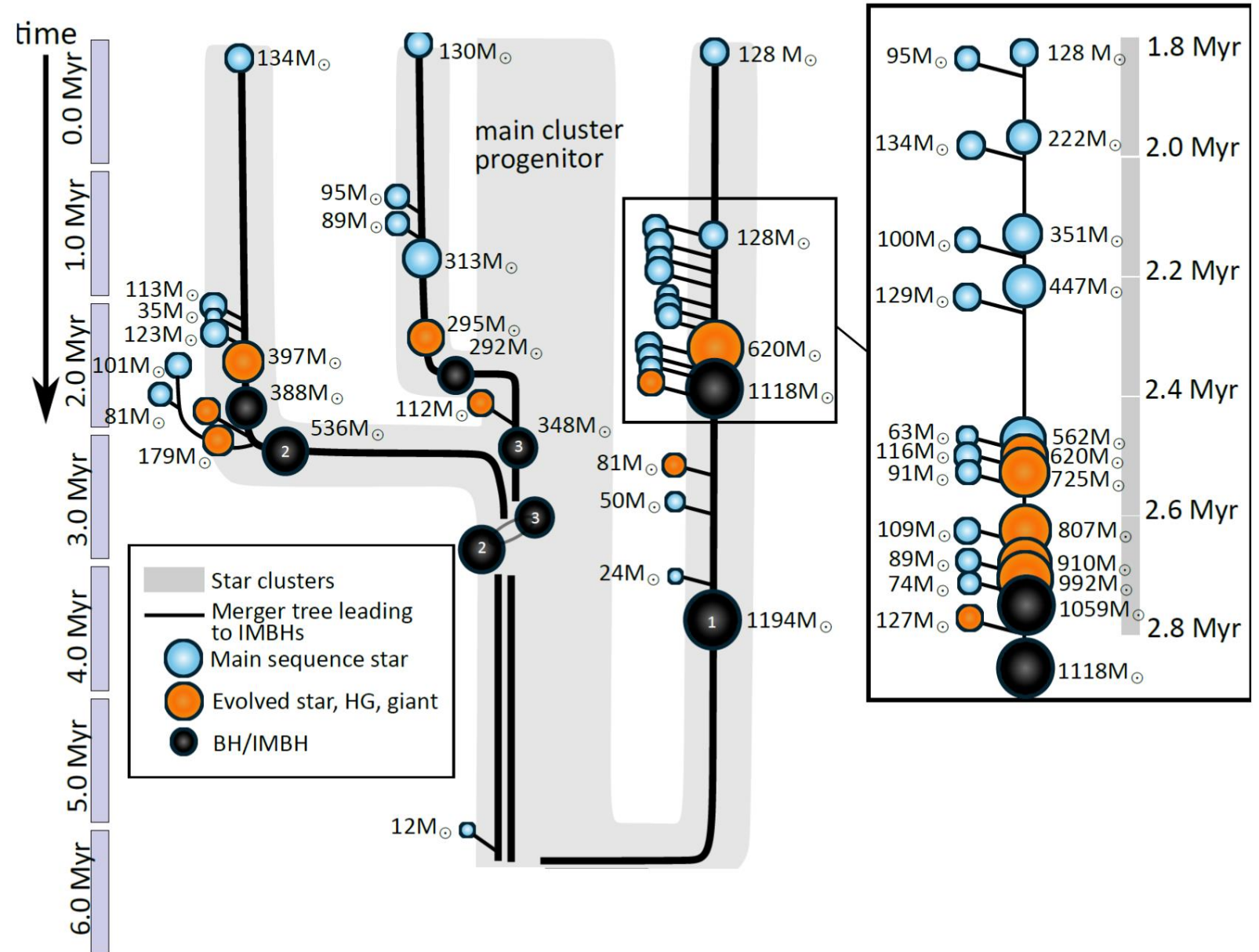
monolithic
star cluster
formation



Star cluster and SMBH seed progenitor star merger trees

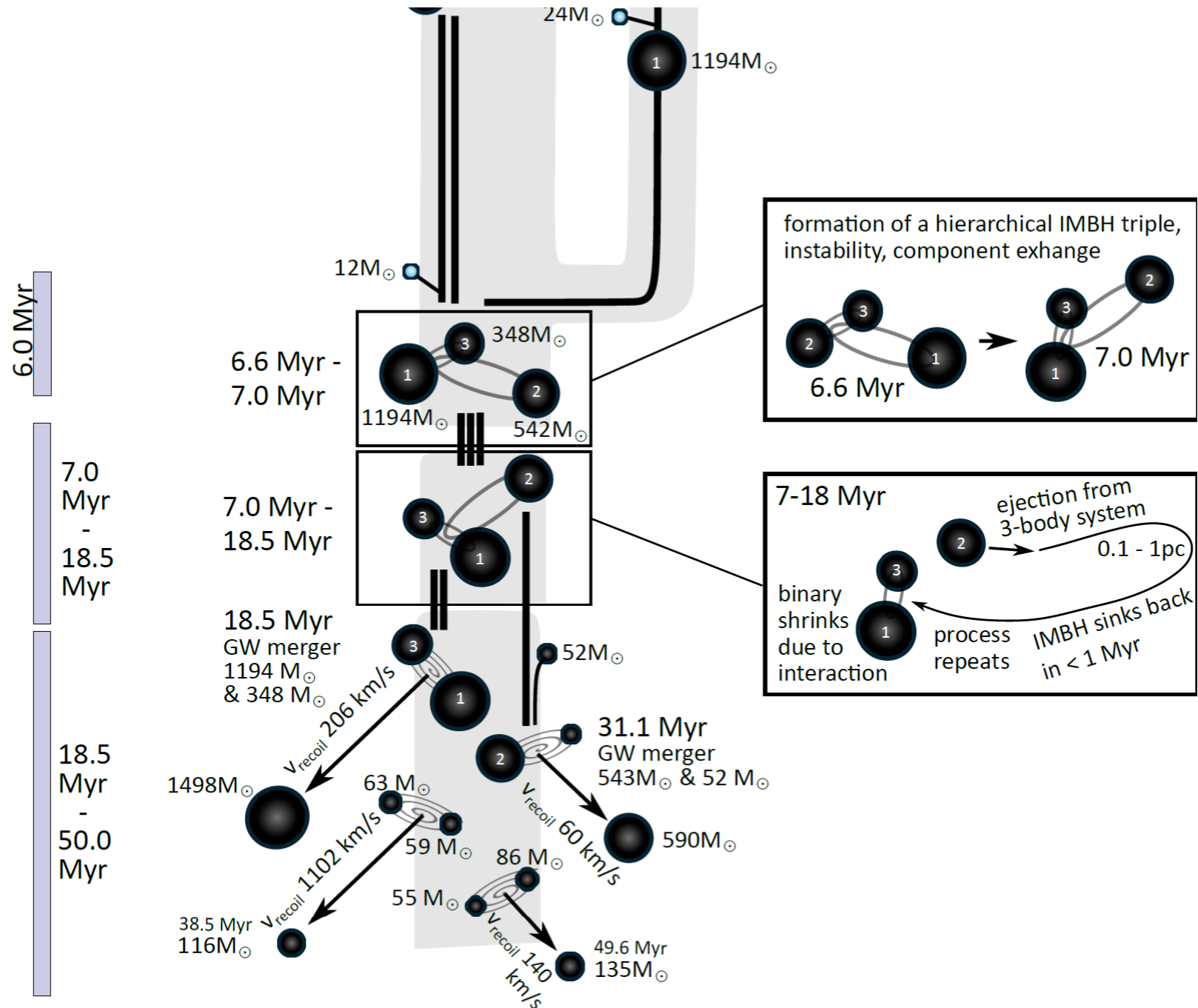


- The collision cascades begin from $>80 M_{\odot}$ stars
- No more than one star per cluster significantly grows by mergers
- Most SMBH seed mass from the stellar collisions, up to $\sim 30\%$ by TDEs and BH-SMBH seed mergers

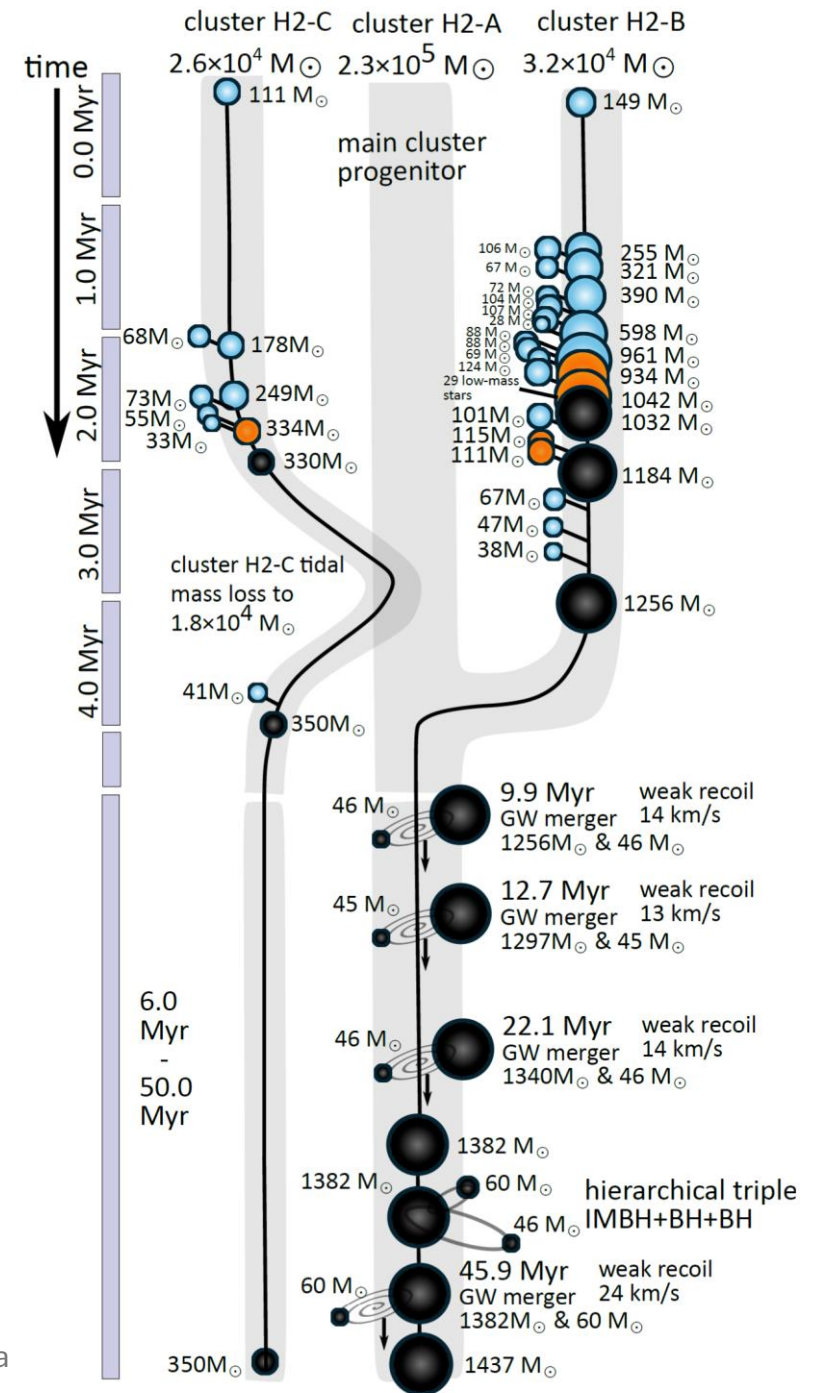


- Complex interaction histories of BHs and SMBH seeds

- seed mergers and GW recoil kicks may eject all seeds from the cluster in this simulation

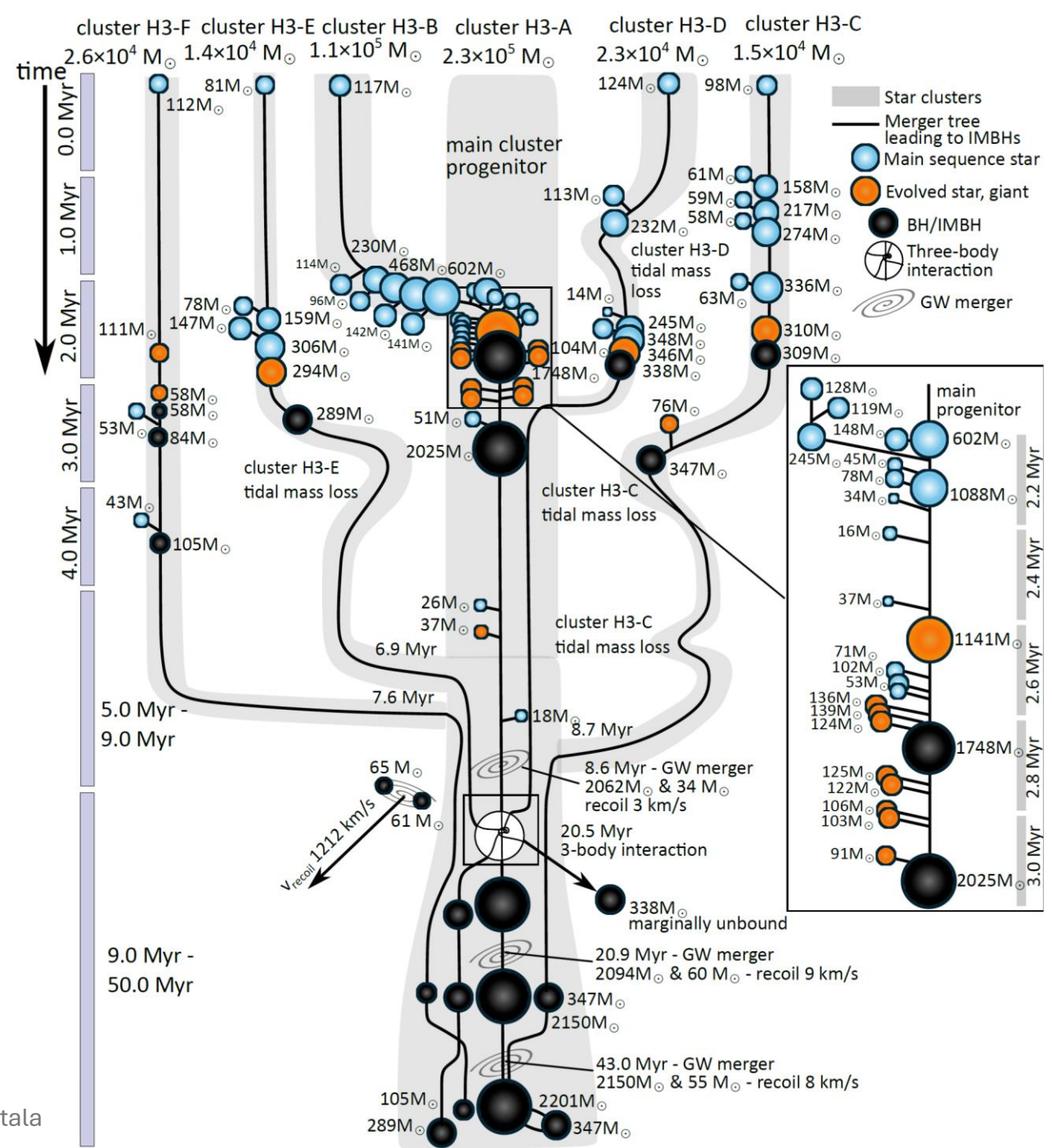


two SMBH seeds, but not in the same star cluster

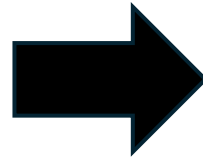


up to five seeds in the same cluster

a number of SMBHs seeds removed by three-body interactions and GW recoil kicks, others remain



Answering the earlier question...



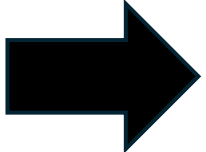
but do young, dense, low-metallicity star clusters look like this?

Answering the earlier question...

FROST-CLUSTERS – I. Hierarchical star cluster assembly boosts
intermediate-mass black hole formation
Antti Rantala^{1*}, Thorsten Naab¹, Natalia Lahén¹
¹Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Str. 1, D-85748, Garching, Germany



Yes, after ~10 Myr...

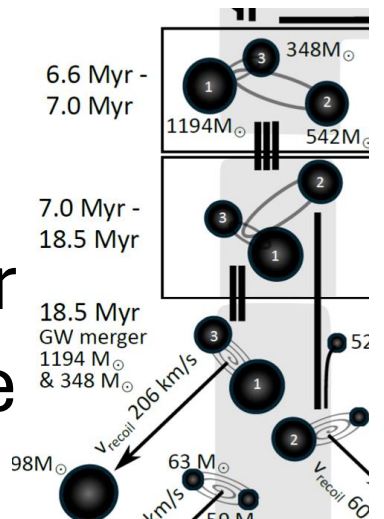


BUT

... the SMBH seed formation has already occurred!

but do young, dense, low-metallicity star clusters look like this?

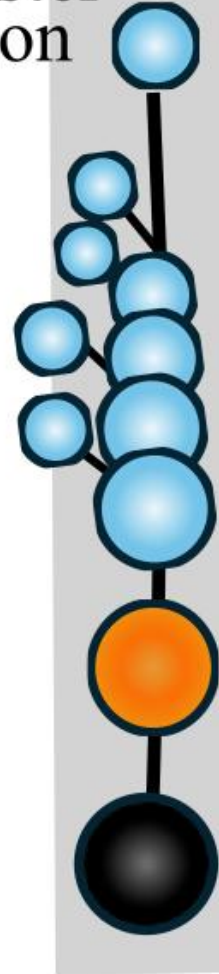
... and the BH content of the cluster is very different to the isolated case!



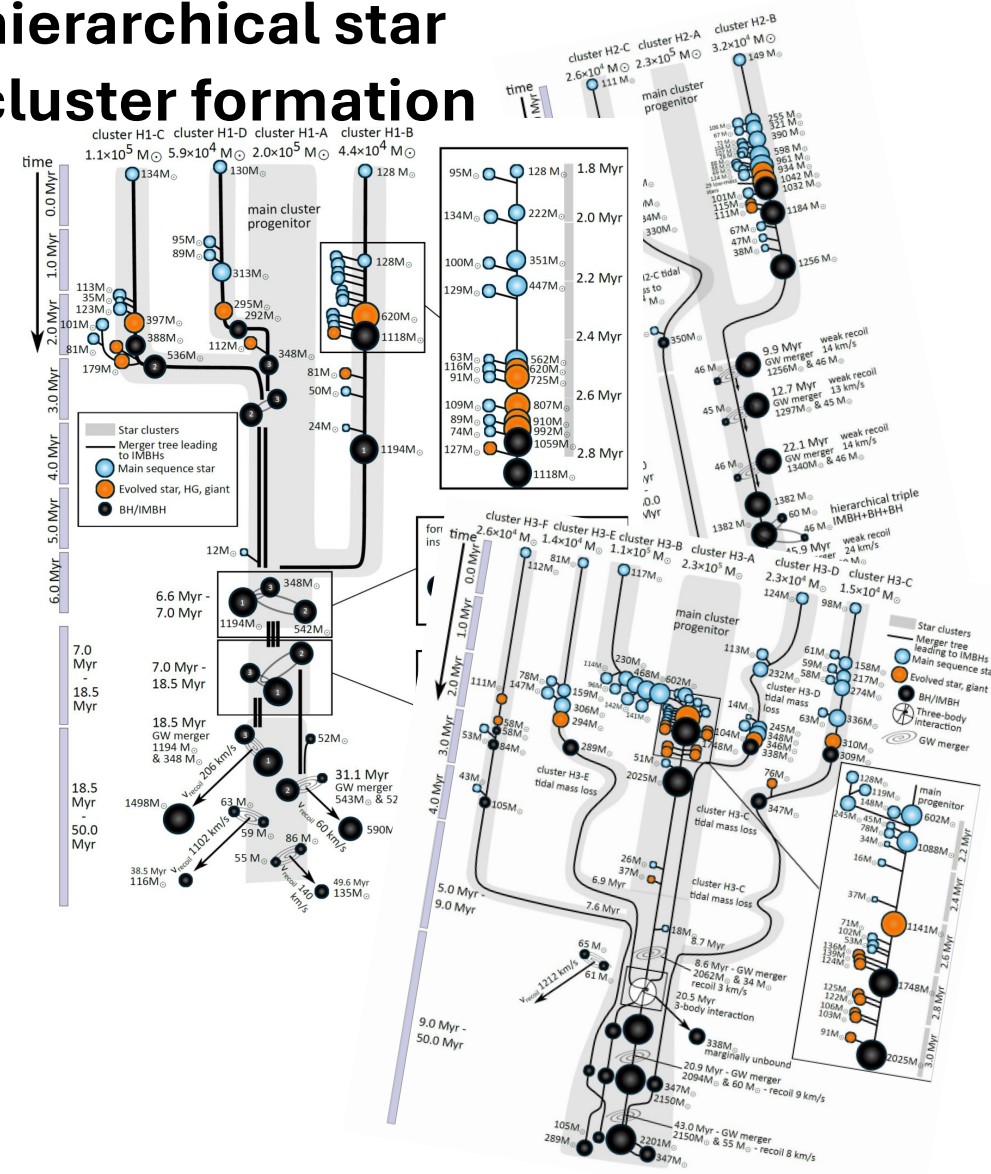
Gravitational waves

- Isolated monolithic and hierarchical assembly setups predict a very different GW fingerprint

monolithic
star cluster
formation

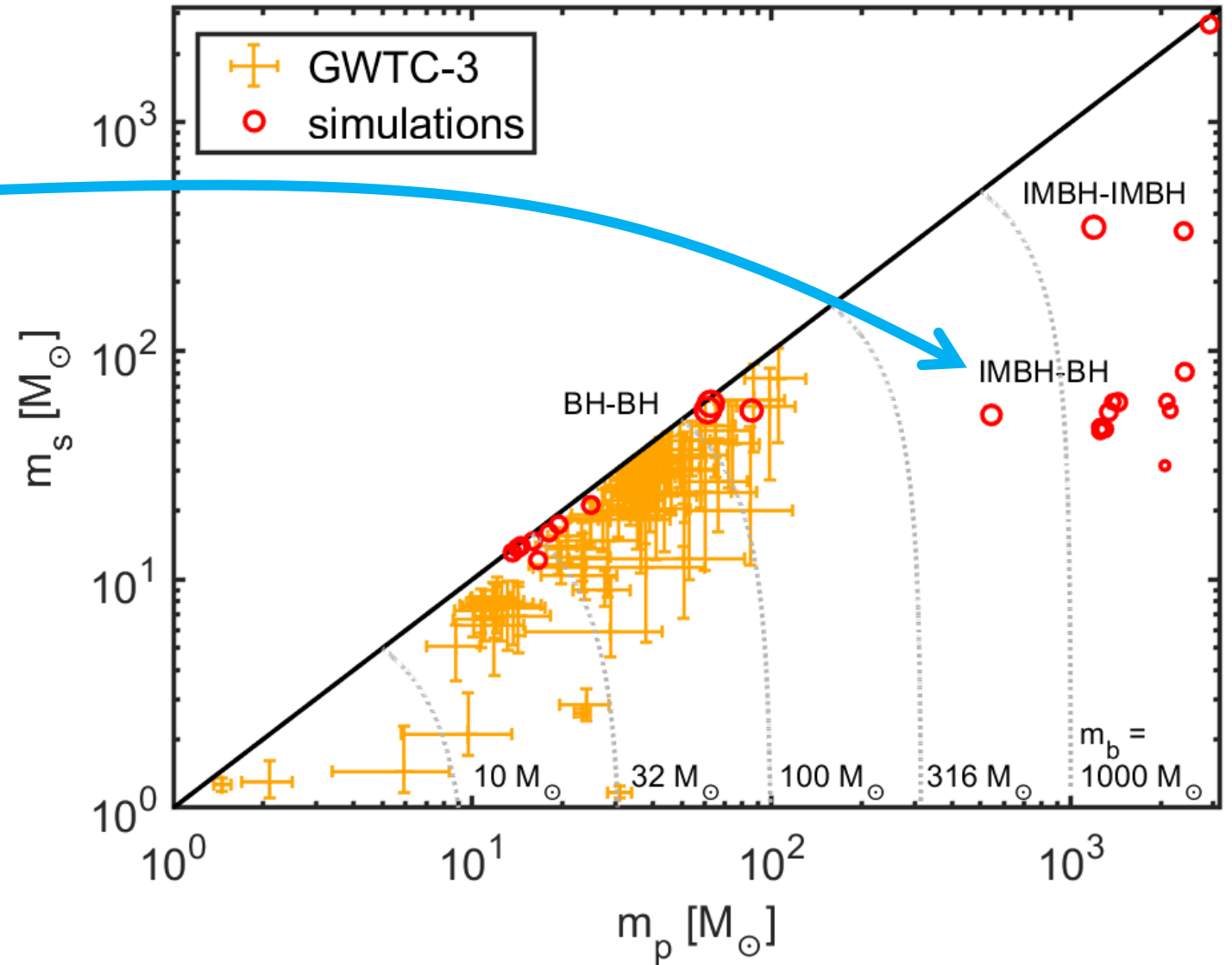


hierarchical star cluster formation



Gravitational waves

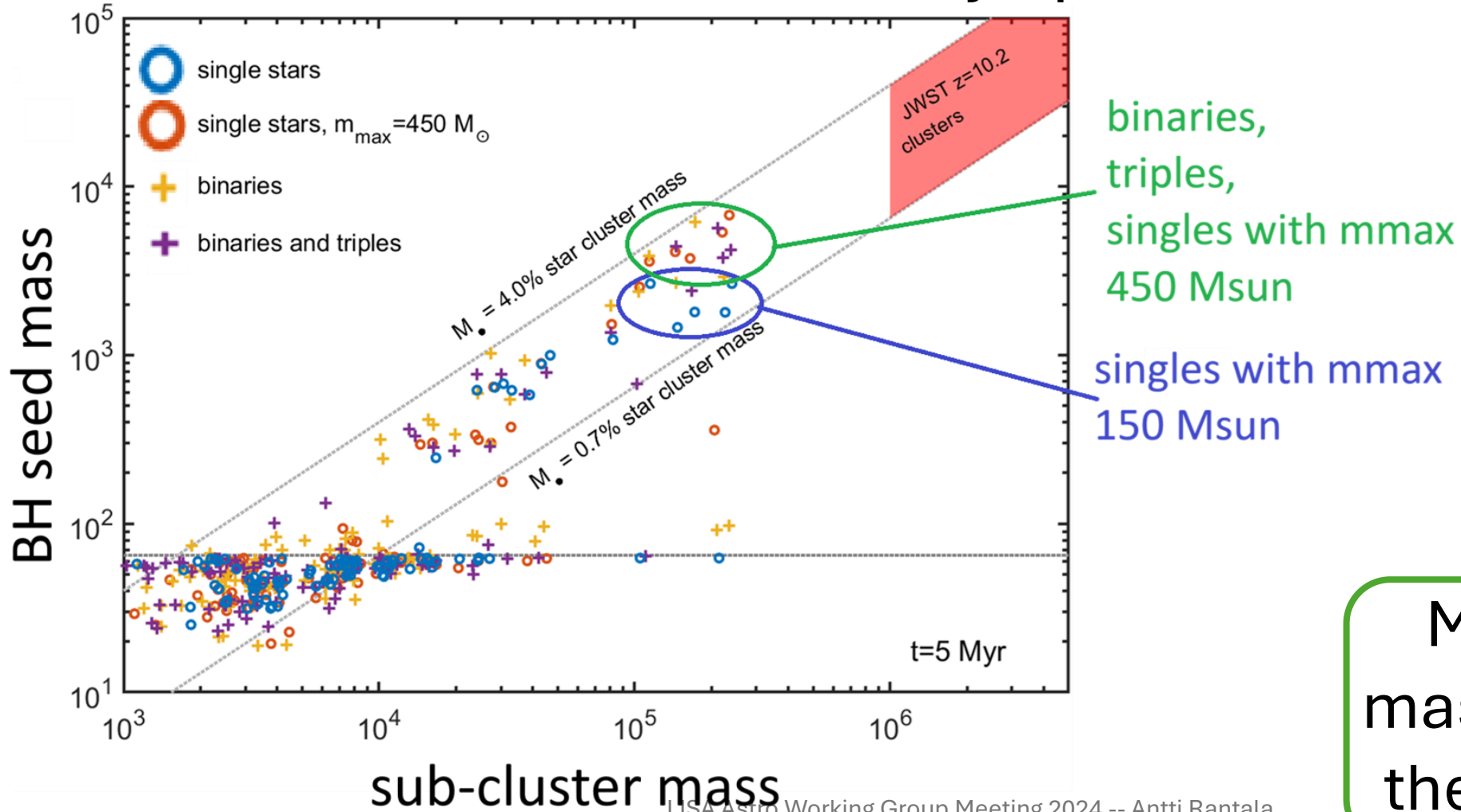
- Simulations predict IMBH GW merger population with $q \sim 1/10$
- Current LIGO/Virgo/KAGRA searches typically up to $\sim 500 M_{\odot}$, cannot observe higher-mass (low-frequency) mergers very well
- LISA, the Einstein Telescope, the Cosmic Explorer



How about binaries... and triples?

Rantala 2024d in prep.

- **Binaries, triples** and **massive singles** increase the SMBH formed seed masses by up to $\sim \times 3$

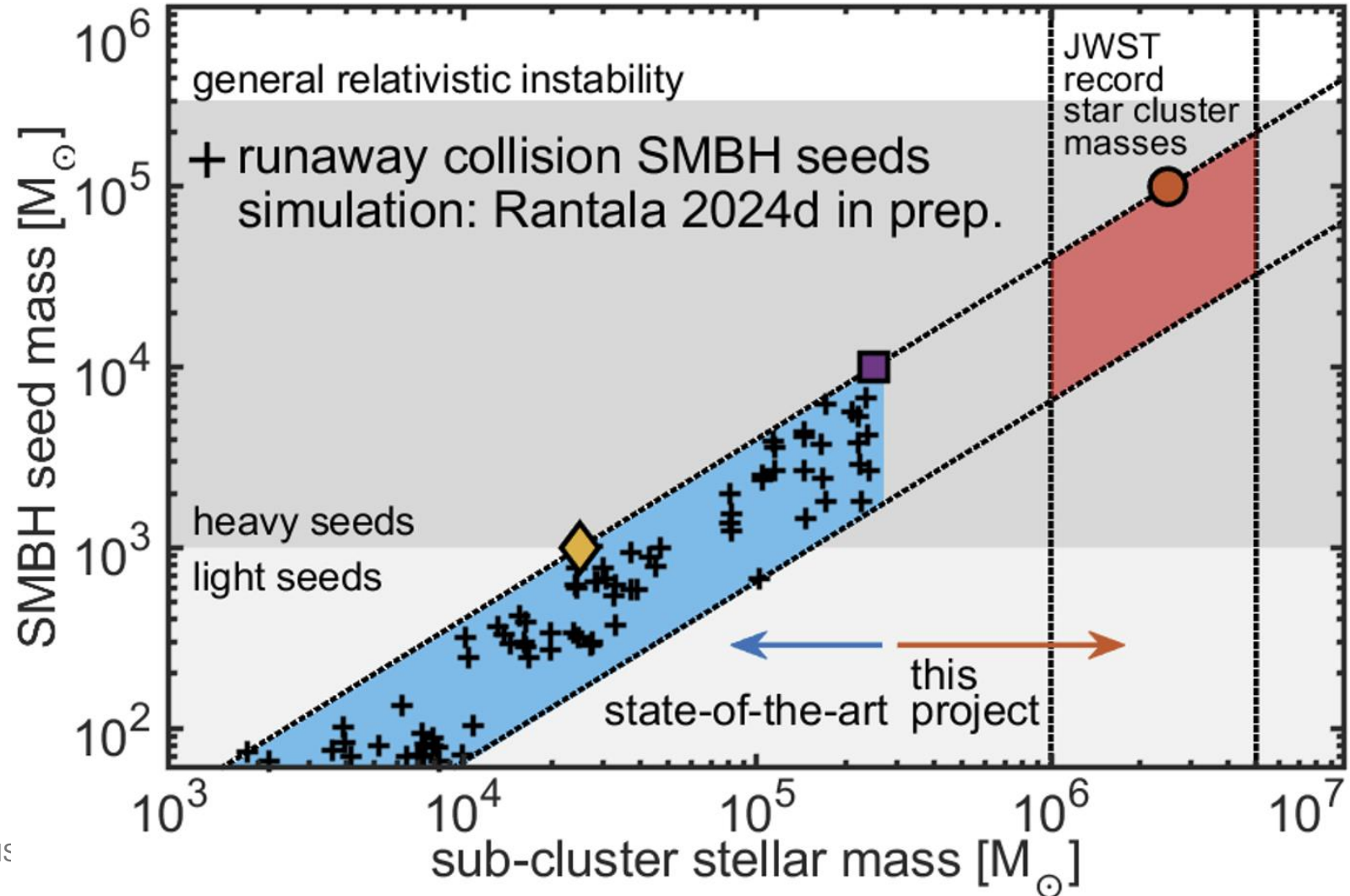
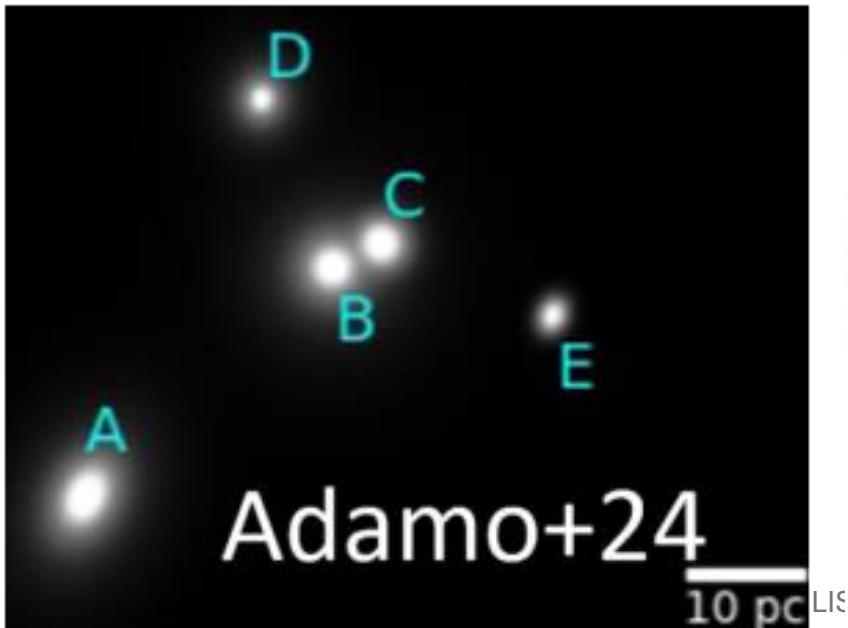


Max SMBH seed mass $\sim 7000 M_{\text{sun}}$ in the current sample

Maximum collisional SMBH seed mass?

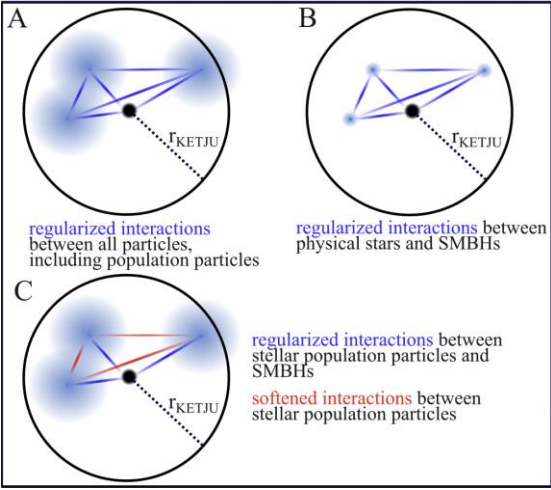
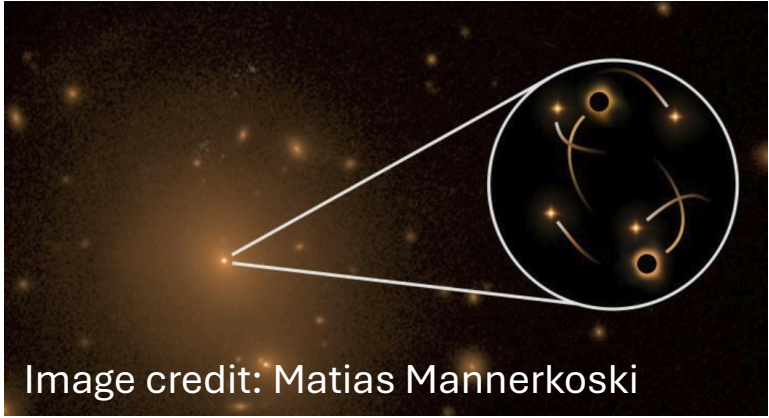
similar %: Gieles+18, Fujii+24

- A few % SMBH seed formation efficiency + JWST $z > 10$ star clusters = ???

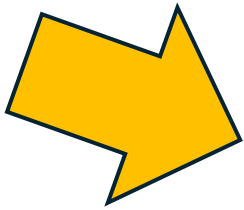


The **KETJU** scaling and speed update

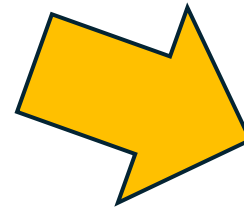
The **KETJU** scaling and speed update



MSTAR
integrator
improvements



Regularized integrator scaling improves from $O(N^2)$ to $O(N)$



Results remain unchanged at 1% level

Removes the speed bottleneck of KETJU simulations

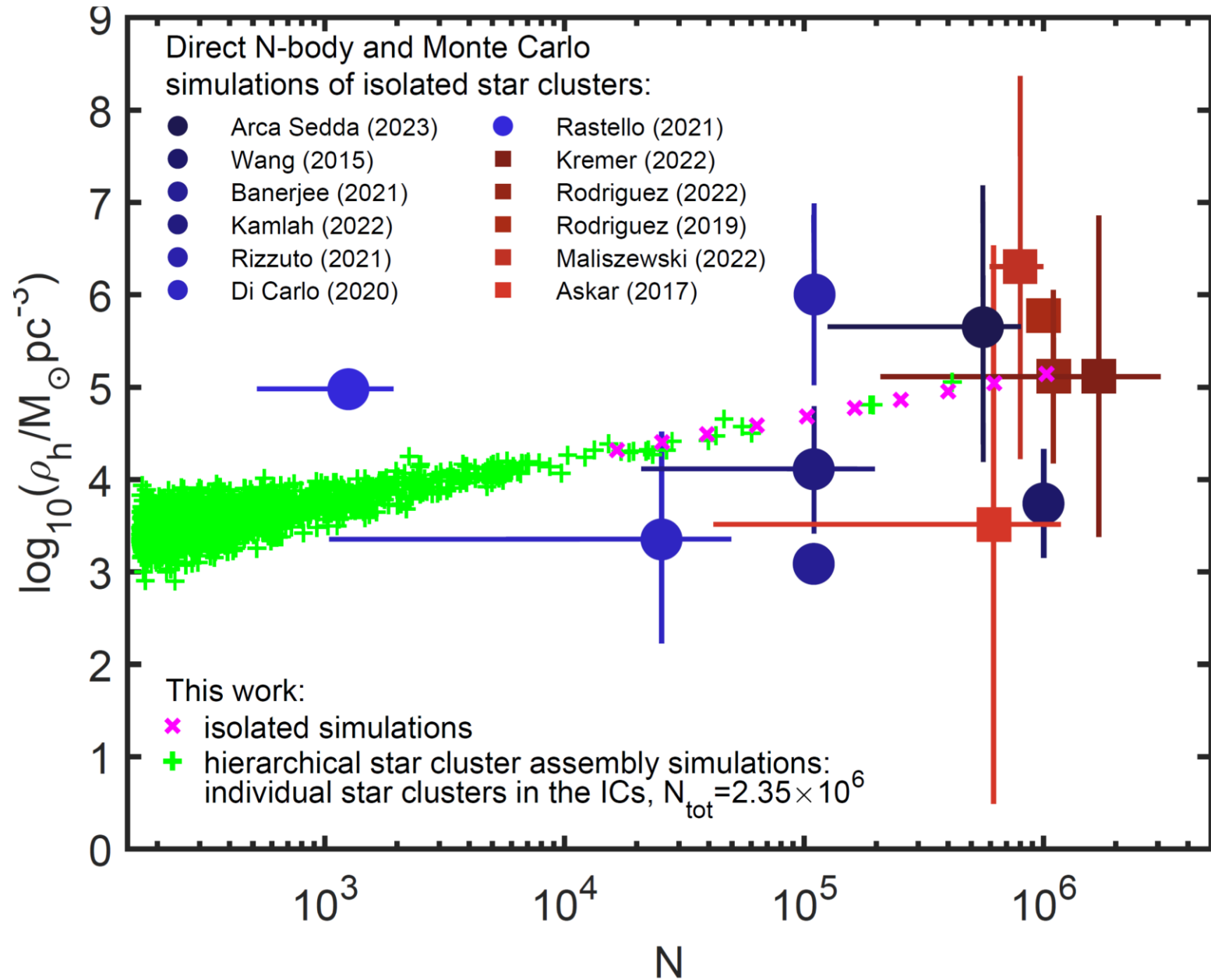
The new fast KETJU will be made publicly available

on the job market this year

anttiran@mpa-garching.mpg.de

Extra slides

Extra slides



Runaway collisions?

- Only the most massive growing objects in each simulation show periods of runaway growth behaviour

